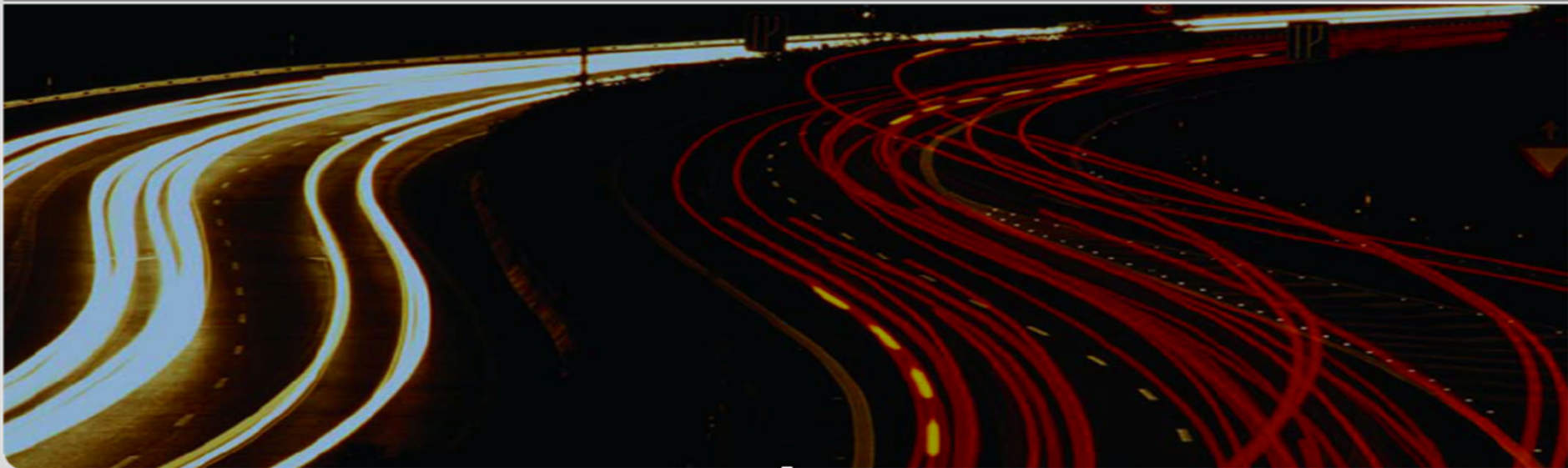


Classical Diversity

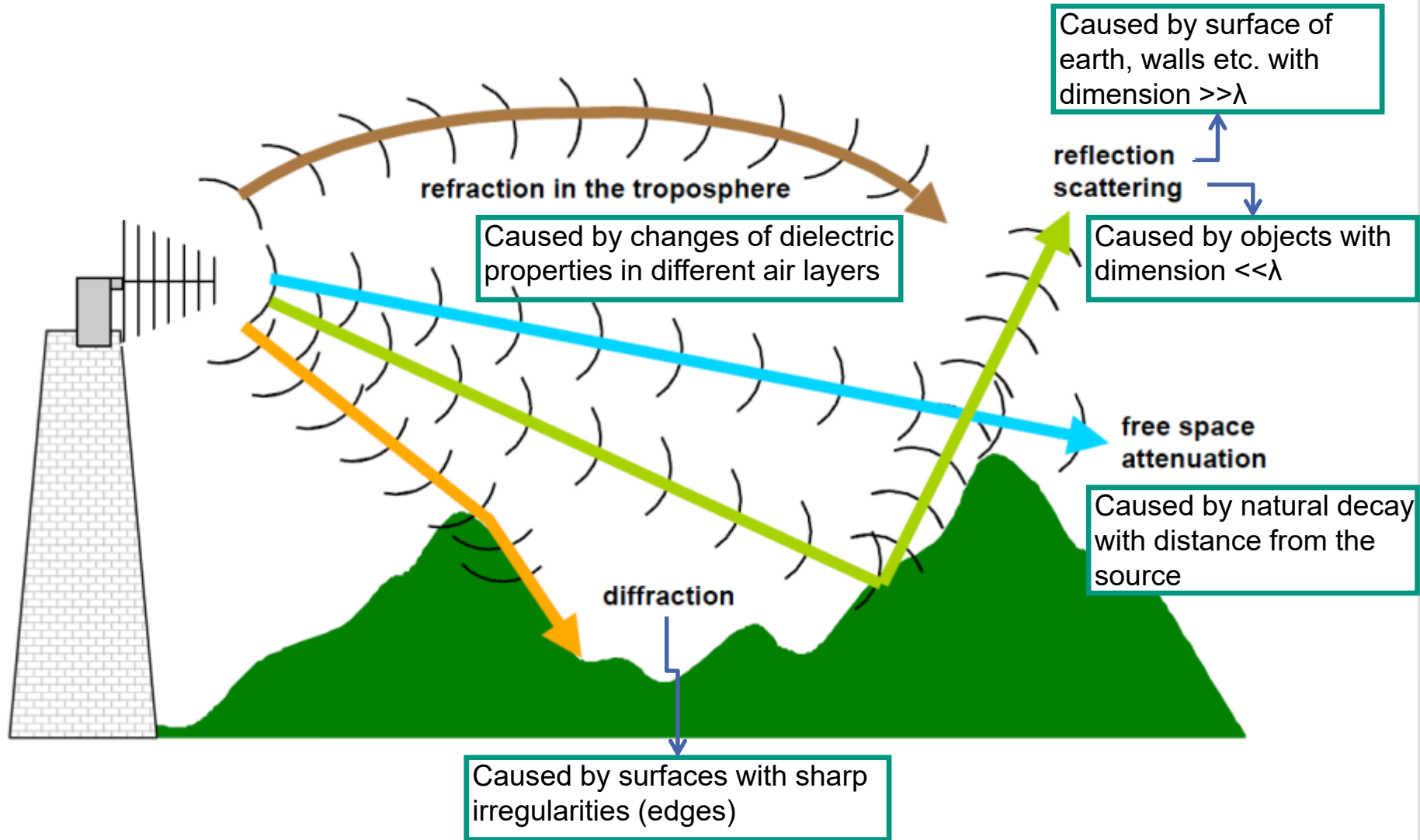
**Thomas Zwick, Lars Reichardt, Christian Sturm, Christian Waldschmidt,
Werner Wiesbeck**

Institut für Hochfrequenztechnik und Elektronik

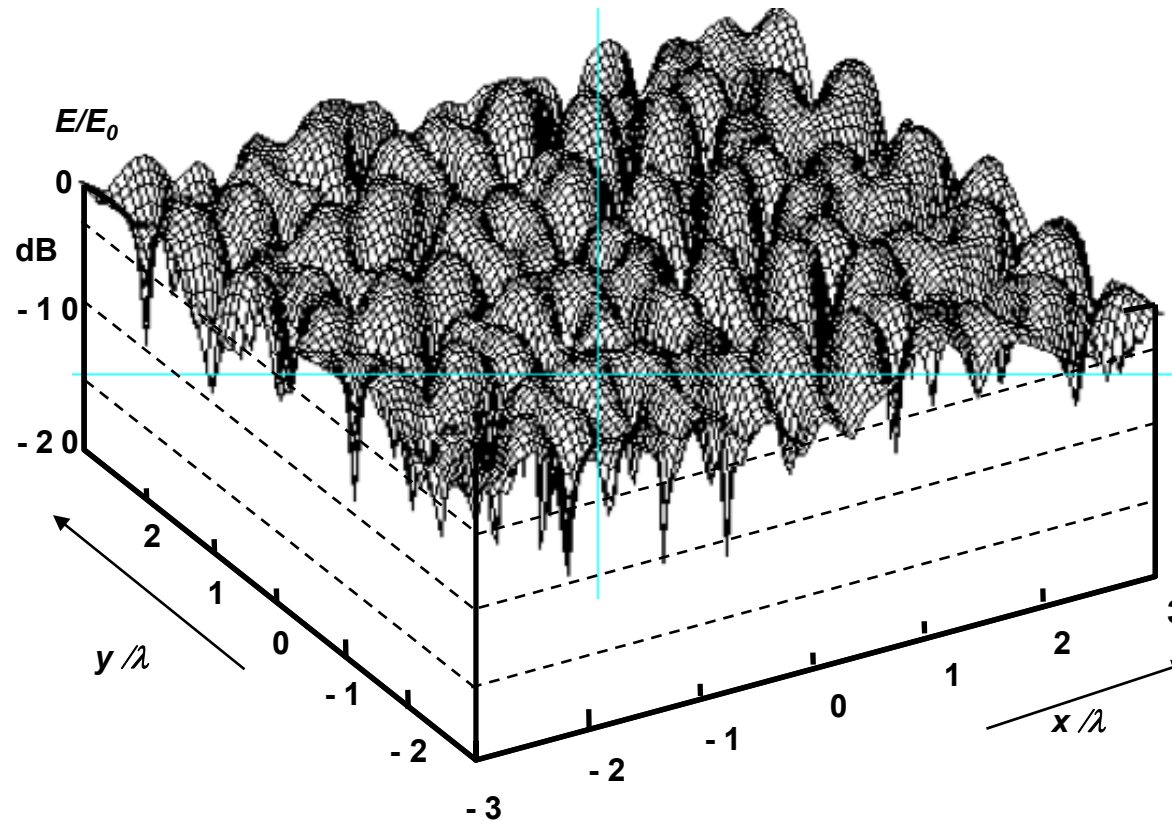


- **The Problem**
- **Fading**
- **Signal Correlation**
- **Diversity Methods**
- **Diversity Combiner**
- **Diversity Efficiency**

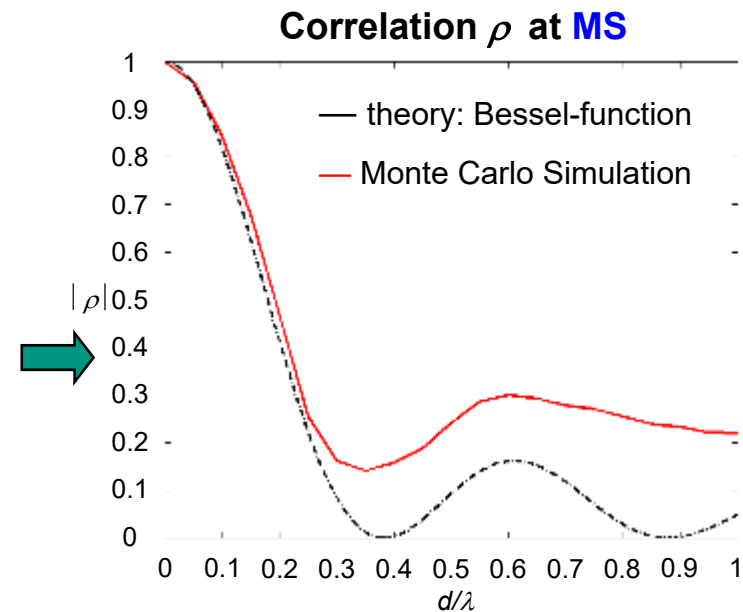
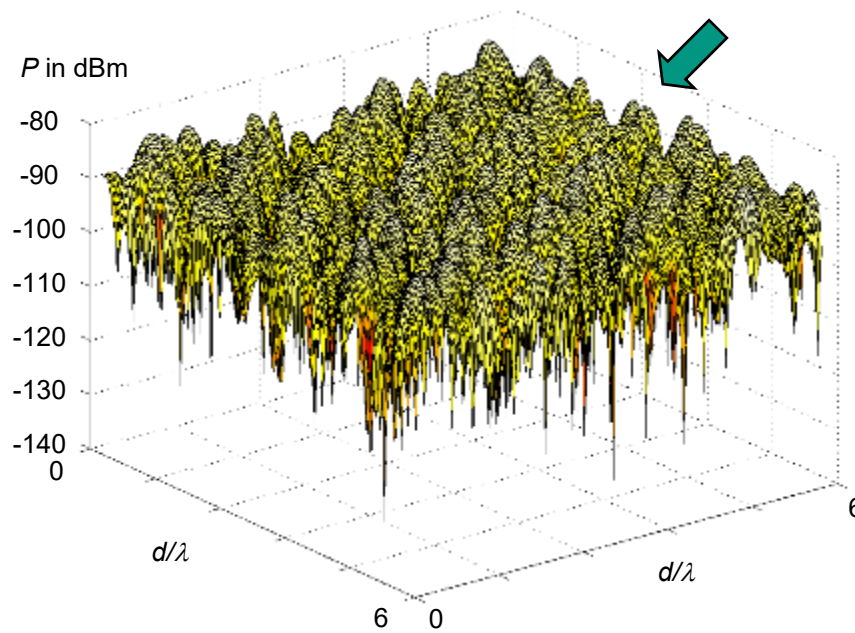
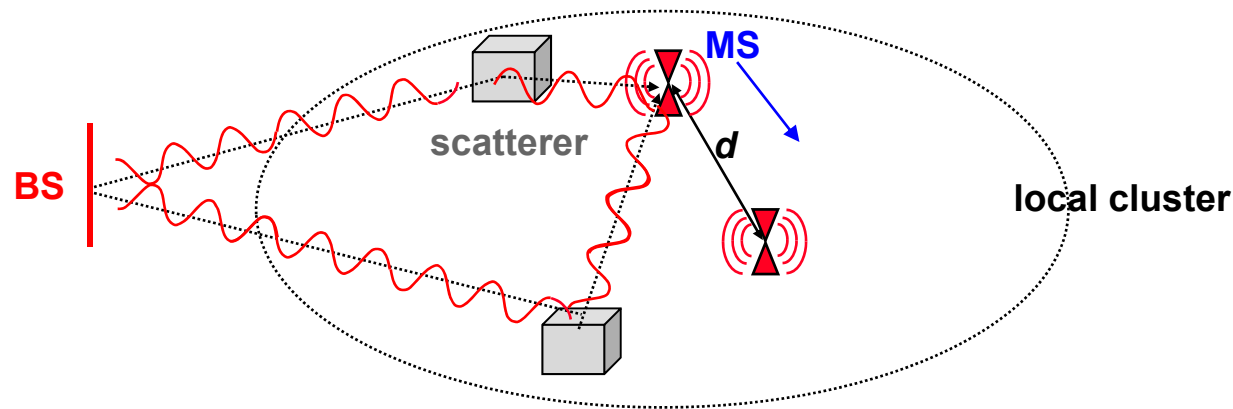
Wave Propagation Phenomena



Relative Signal Strength in a Multi-Path



Relative Power in a Multi-Path Environment



Task of Diversity:

Diversity is a means to overcome the **fading** problem by multiple receiving subsystems.

Principle of Diversity:

The principle of diversity is to **select or combine** the multiple **received** signals in a way that the resulting signal is always better than, or equal to, the better one of the single signals.

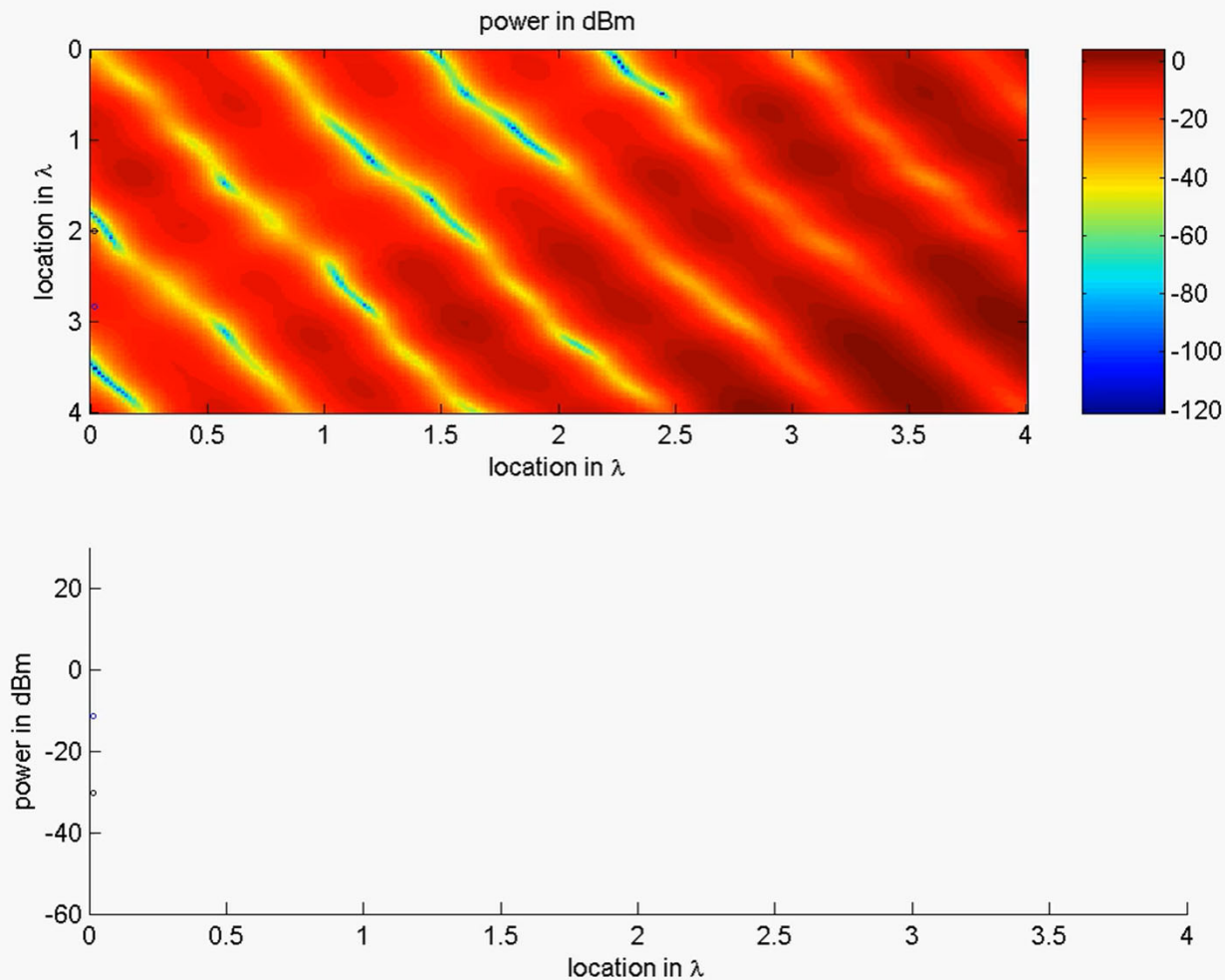
Requirements:

- similar average signal strength in all channels
- similar average noise in all channels
- low correlation of the receive channels

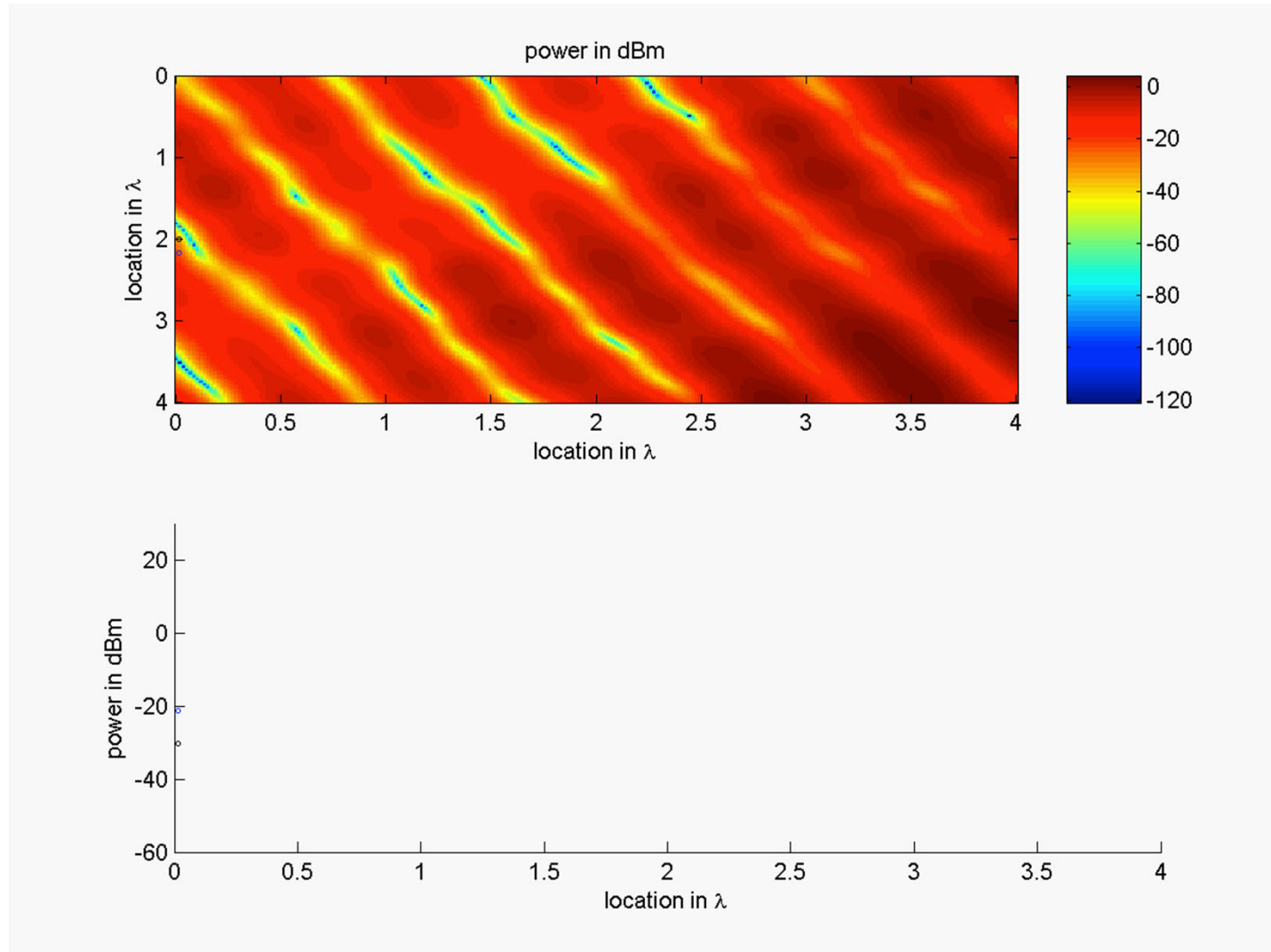
Assumptions:

- signal independent additive noise
- uncorrelated noise
- signal amplitude is Rayleigh distributed

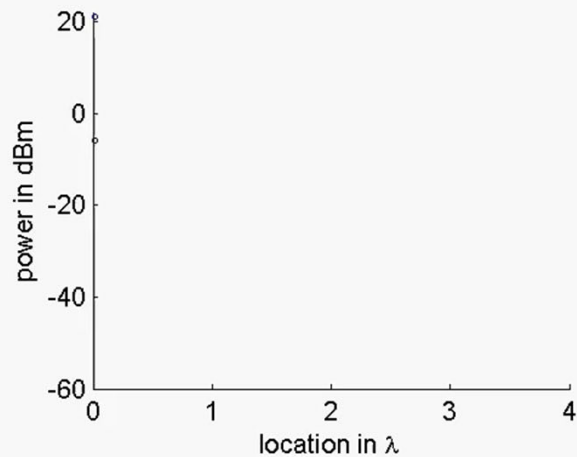
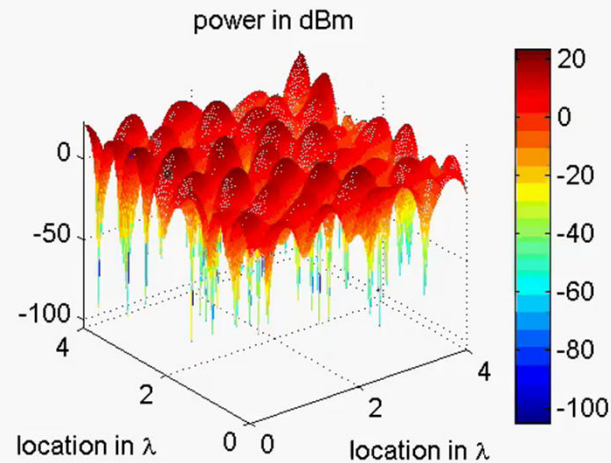
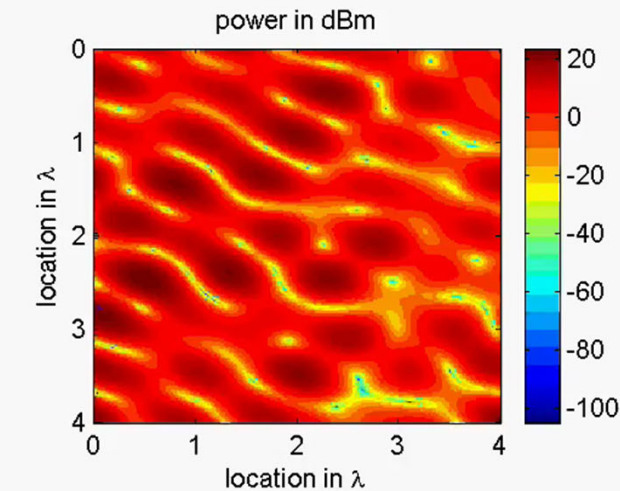
Space Diversity, Antenna Separation $d = 0.7\lambda$



Diversity with Small Antenna Separation, $d = 0.05\lambda$

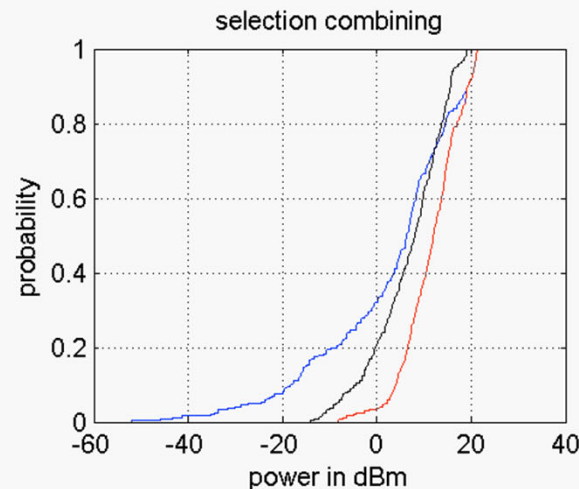
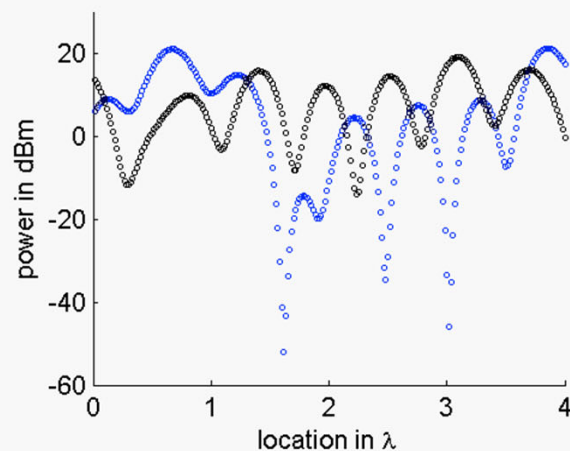
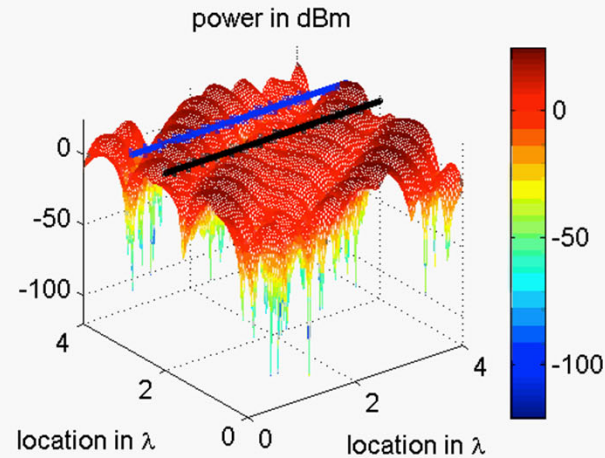
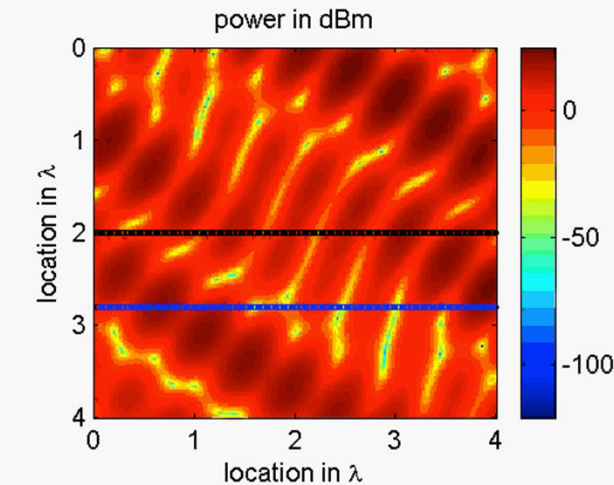


Diversity with Wide Antenna Separation, $d = 0,7\lambda$



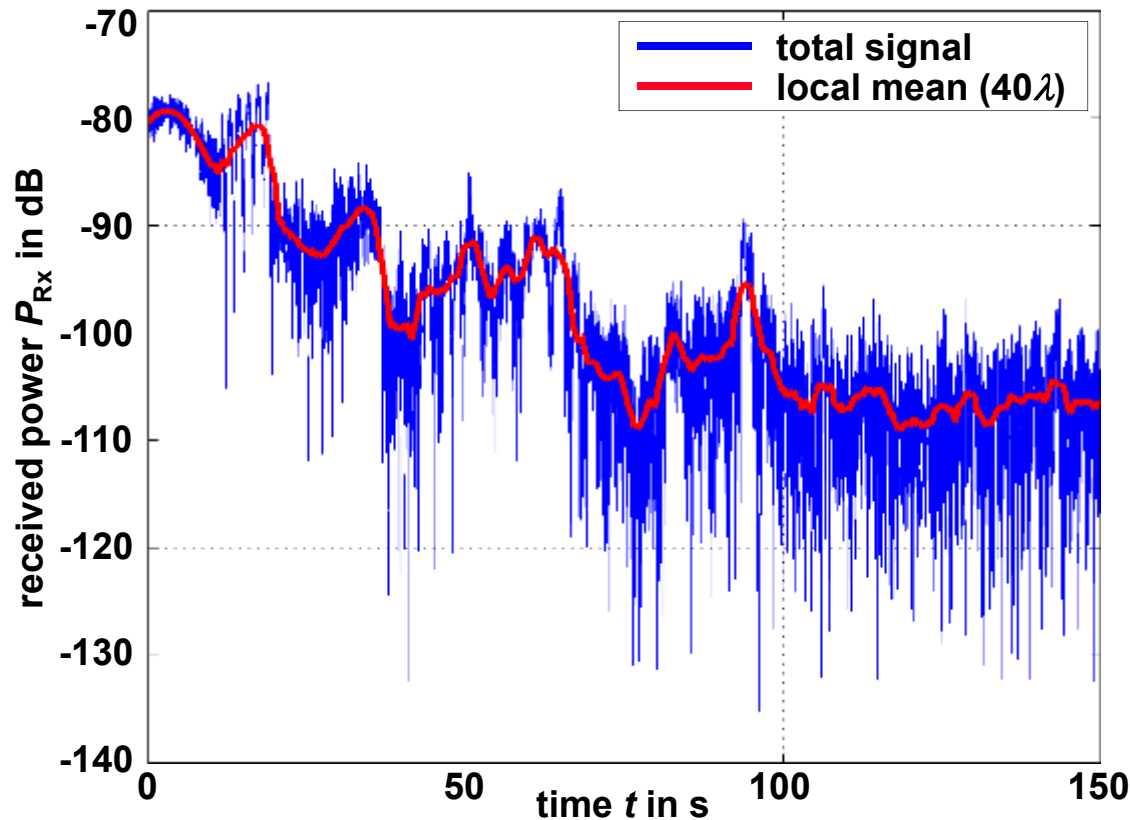
- signal no. 1
- signal no. 2
- combined signal

Diversity with Wide Antenna Separation, $d = 0,7\lambda$



- signal no. 1
- signal no. 2
- combined signal

Components of Fading (Narrow-Band Analysis)



receive signal transfer function
at single carrier frequency:

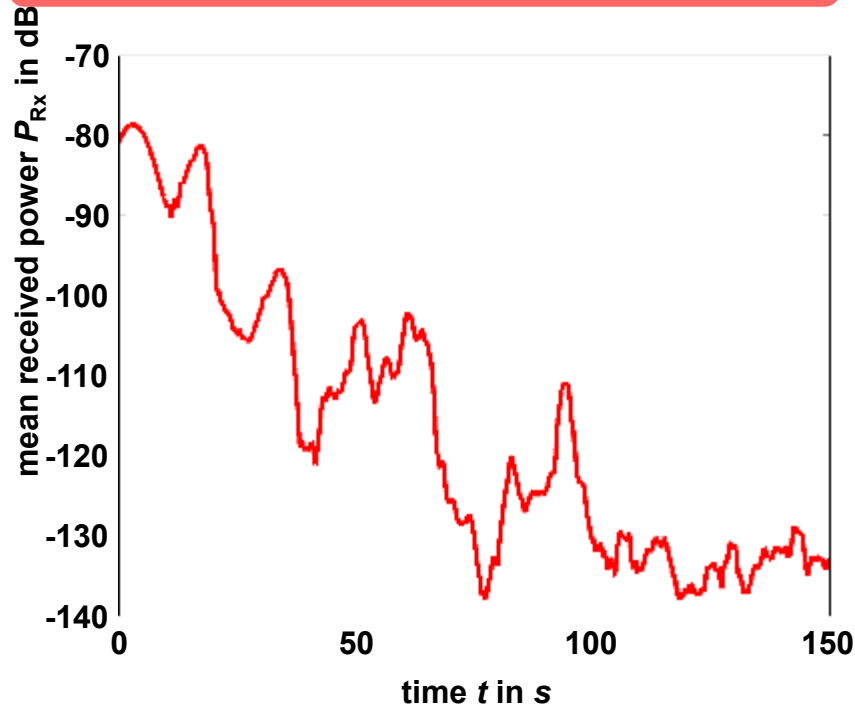
$$|H^{TP}(t)| = l(t) \cdot s(t)$$

$l(t)$: long-term fading
➤ absolute values

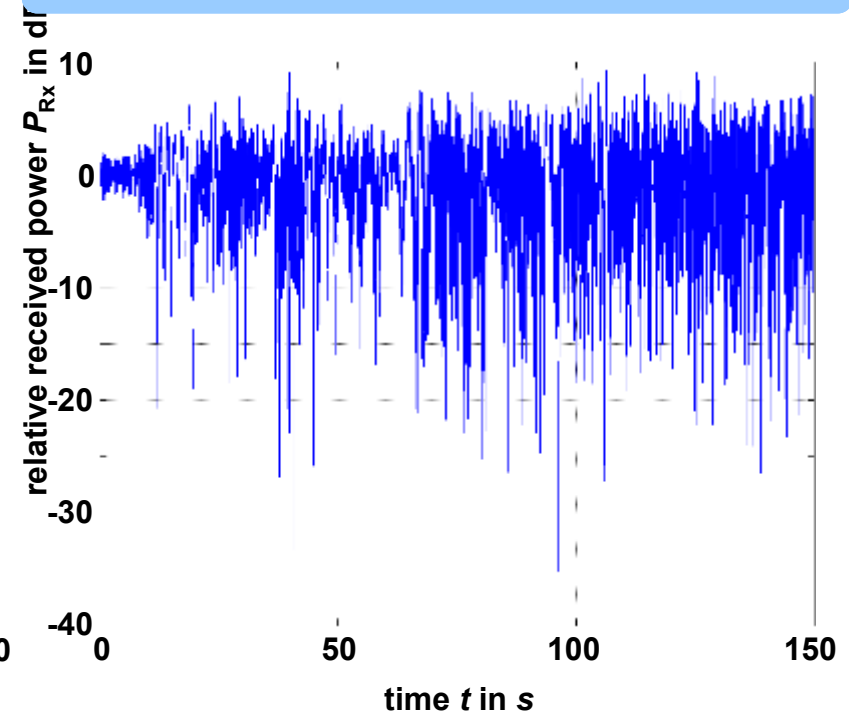
$s(t)$: short-term fading
➤ statistical parameters

Long-Term Fading & Short-Term Fading

long-term fading $l(t)$



short-term fading $s(t)$

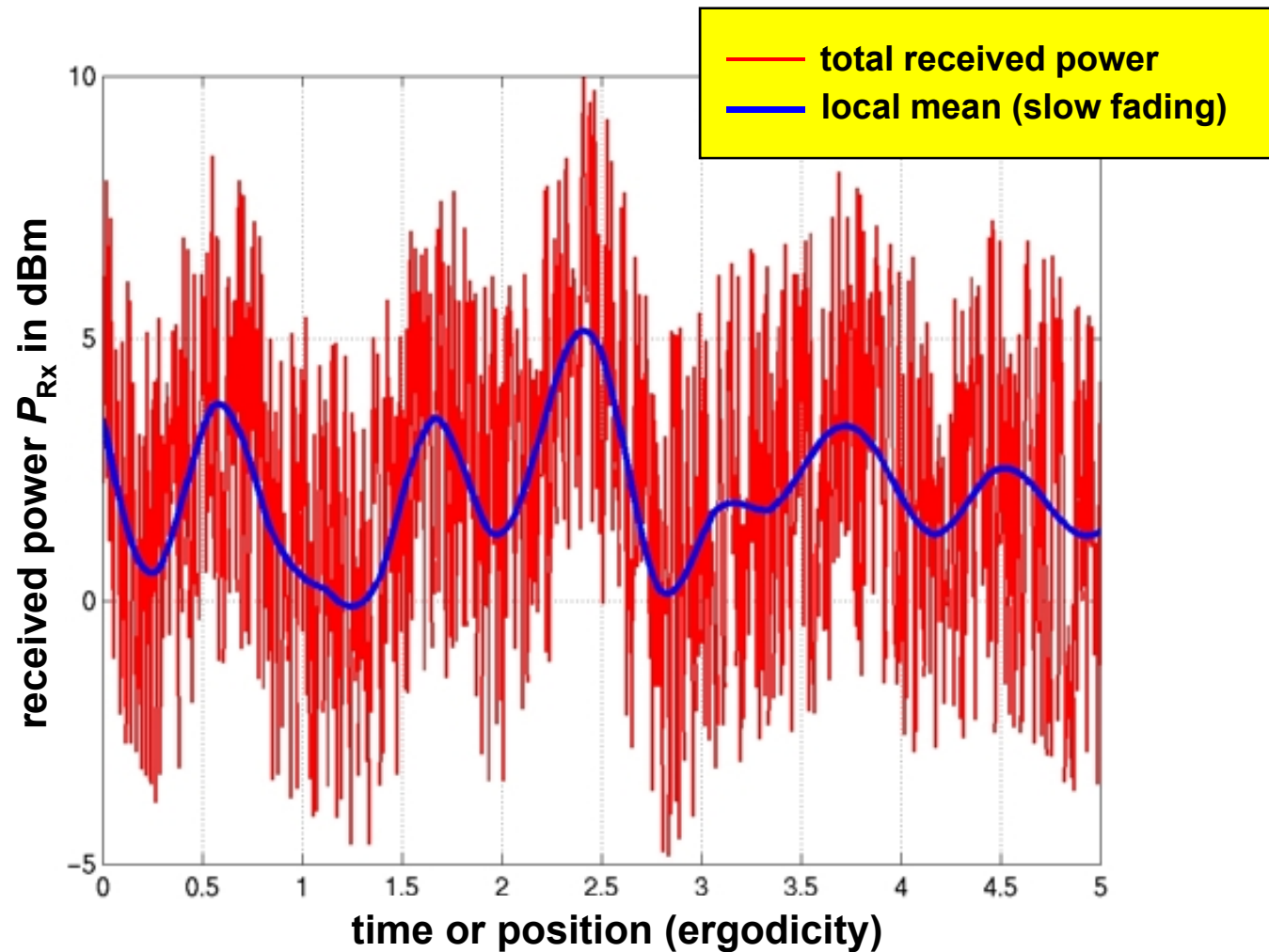


$$l(t) = \frac{1}{2w} \int_{t-w}^{t+w} |H^{TP}(t)| dt; \quad l(t_k) = \frac{\sum_{i=t_k-w_{t_k}}^{t_k+w_{t_k}} |H^{TP}(i)|}{2w_{t_k} + 1}$$

$$s(t) = \frac{|H^{TP}(t)|}{l(t)}; \quad s(t) = \frac{|H^{TP}(t_k)|}{l(t_k)}$$

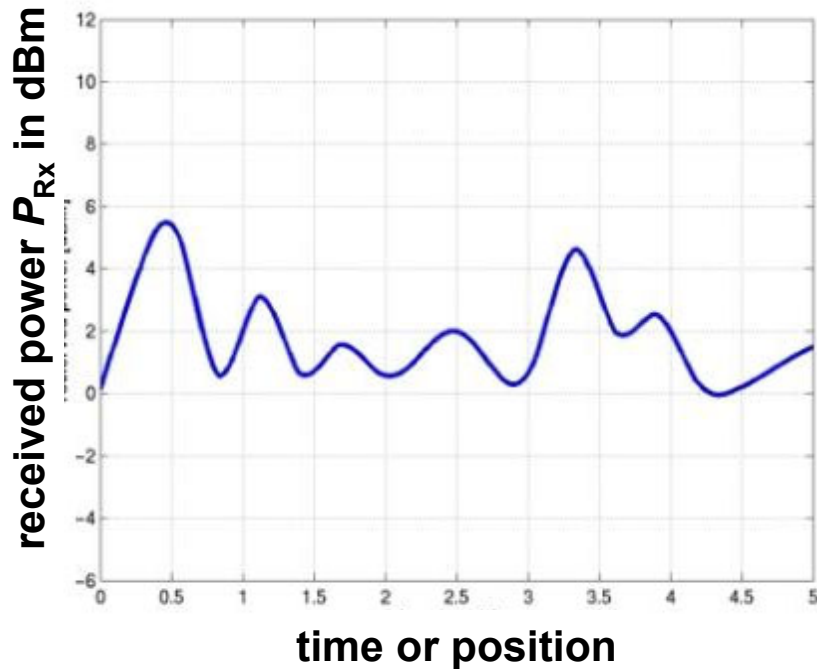
$$\text{window } w : w = \frac{w_\lambda \cdot c_0}{v \cdot f_0}; \quad \text{discret : } w_{t_k} = w \cdot f_{\text{sampling}}$$

Small-Scale (Fast) & Large-Scale (Slow) Fading

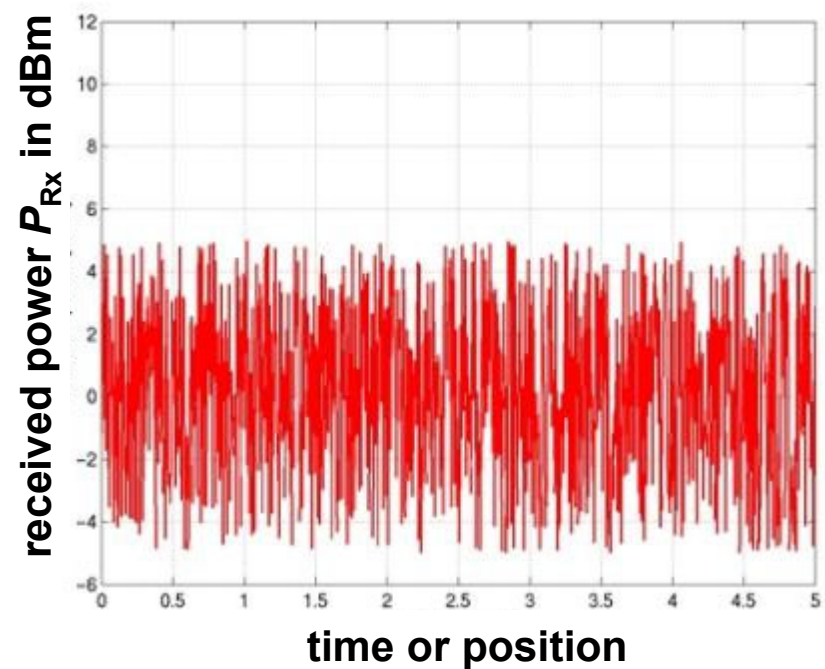


The Components of Fading

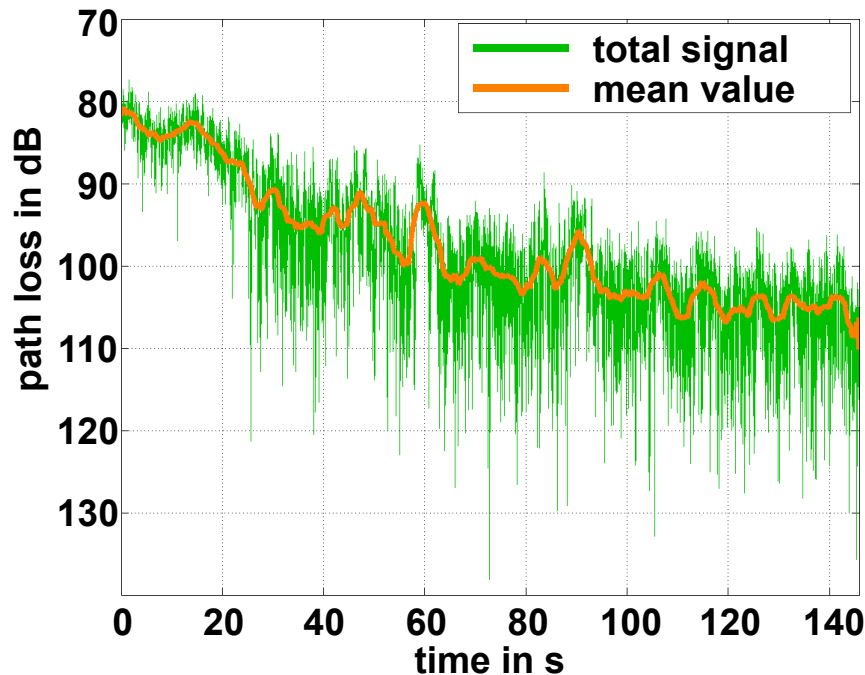
Long-term fading $I(t)$
(slow fading)



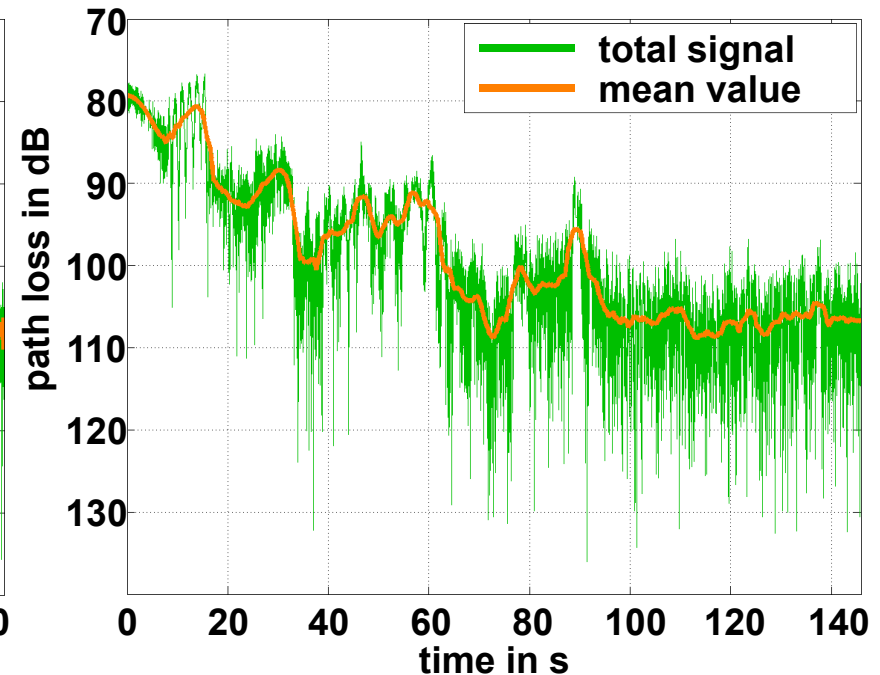
Short-term fading $s(t)$
(fast fading)



measurement



simulation



$$s(t) = l(t) \cdot s(t)$$

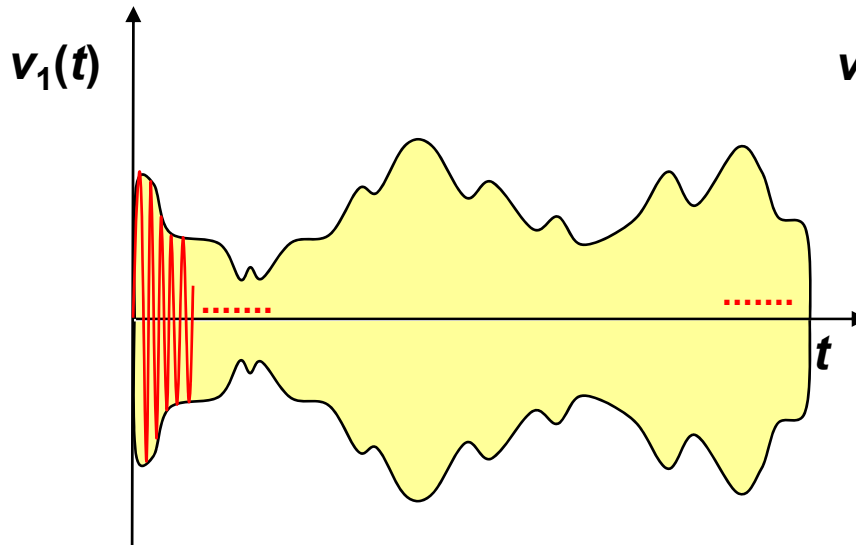
$l(t)$: long-term fading
→ absolute values

$s(t)$: short-term fading
→ statistical parameters

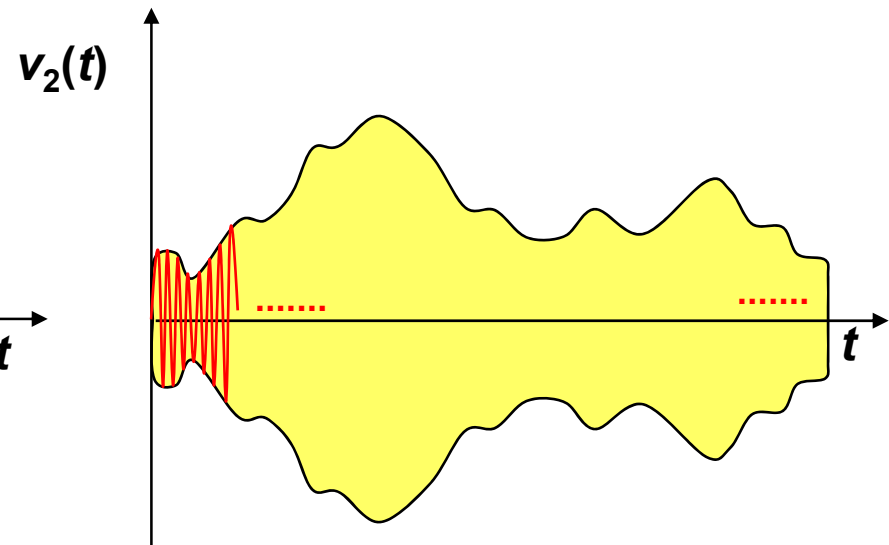
Multi-path in the radio channel creates ***short-term fading*** effects. This results in:

- rapid changes in signal strength over a small travel distance or time interval
- frequency selectivity caused by multi-path propagation delays
- frequency modulation due to varying Doppler shifts on different multi-path signals

Signals in two Diversity Receiving Channels



$$v_1(t) = a_1(t) \cdot \cos(\omega t + \varphi_1(t))$$



$$v_2(t) = a_2(t) \cdot \cos(\omega t + \varphi_2(t))$$

The antenna ν output voltage $\underline{V}_\nu$ results from N incident waves for a position $\vec{x}$:

$$\underline{V}_\nu(\vec{x}) \approx \sum_{i=1}^N \underline{C}_\nu(\theta_i, \psi_i) \cdot \vec{E}_i e^{-j\omega\tau_i} e^{-jk_i \vec{x}}$$

$$\underline{C}_\nu(\theta_i, \psi_i) = \underline{C}_{\theta_\nu}(\theta_i, \psi_i) \cdot \vec{e}_\theta + \underline{C}_{\psi_\nu}(\theta_i, \psi_i) \cdot \vec{e}_\psi$$

$$\vec{E}_i = |\vec{E}_{\theta i}| e^{-j\varphi_{\theta i}} \cdot \vec{e}_\theta + |\vec{E}_{\psi i}| e^{-j\varphi_{\psi i}} \cdot \vec{e}_\psi$$

$$\vec{k}_i = -k \sin \theta_i \cdot \cos \psi_i \cdot \vec{e}_x - k \sin \theta_i \cdot \sin \psi_i \cdot \vec{e}_y - k \cos \theta_i \cdot \vec{e}_z$$

$\underline{C}_{\theta_\nu}(\theta, \psi)$ and $\underline{C}_{\psi_\nu}(\theta, \psi)$ define the polarization dependent complex far field antenna pattern of the receive antenna ν

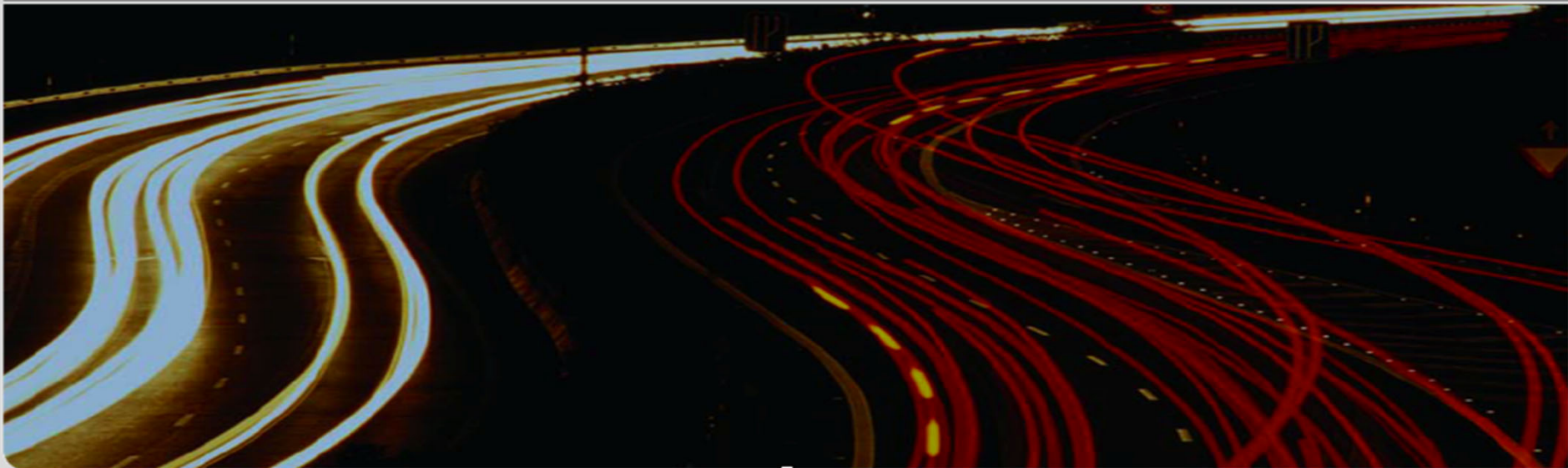
For two antennas the output voltages $v_\nu(t)$ and $v_\mu(t)$ are:

$$v_\nu(t) = a_\nu(t) \cdot \cos(\omega t + \varphi_\nu(t))$$

$$v_\mu(t) = a_\mu(t) \cdot \cos(\omega t + \varphi_\mu(t))$$

Received Signals Correlation of Diversity and MIMO Antenna Systems

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Received signal amplitude A at antenna i or j :

$$\underline{A}_{i,j}(t)$$

Received power P at antenna i or j :

$$P_{i,j}(t)$$

Received mean signal at antenna i or j :

$$m_{i,j}$$

Amplitude Standard Deviation at antenna i or j :

$$\sigma_{A_{i,j}}$$

Power Standard Deviation at antenna i or j :

$$\sigma_{P_{i,j}}$$

Incident field-strength: $E(\theta, \psi)$; Incident power density: $S(\theta, \psi)$

Envelope-Covariance-Coefficient ρ_{Aij}

Normalized Amplitude-Cross-Correlation-Coefficient

$$\rho_{Aij} = \frac{R_{Aij}}{\sigma_{Ai} \sigma_{Aj}}$$

Amplitude Cross Correlation

$\sqrt{\text{Variances of } A_{pi,j}}$

$$R_{Aij} = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^{+T} \left(\left| \langle \underline{A}_i(t) \rangle \right| - m_i \right) \left(\left| \langle \underline{A}_j(t) \rangle \right| - m_j \right) dt$$

$$\sigma_{Ai,j} = \sqrt{\lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^{+T} \left(\left| \langle \underline{A}_{i,j}(t) \rangle \right| - m_{i,j} \right)^2 dt}$$

$$m_{Ai,j} = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^{+T} \left| \langle \underline{A}_{i,j}(t) \rangle \right| dt$$

Power-Covariance-Coefficient ρ_{Pij}

Normalized Power-Cross-Correlation-Coefficient

$$\rho_{Pij} = \frac{R_{Pij}}{\sigma_{Pi}\sigma_{Pj}}$$

Power Cross
Correlation

$\sqrt{\text{Variances of } P_{pi,j}}$

$$R_{Pij} = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^{+T} (P_{Pi}(t) - m_{Pi})(P_{Pj}(t) - m_{Pj}) dt$$

$$\sigma_{Pi,j} = \sqrt{\lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^{+T} (P_{Pi,j}(t) - m_{Pi,j})^2 dt}$$

$$m_{Pi,j} = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^{+T} P_{Pi,j}(t) dt$$

$$\rho_{Pij} \approx |\rho_{Aij}|^2 = \frac{|R_{ij}|^2}{\sigma_i \sigma_j}$$

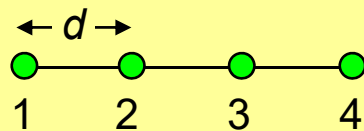
$$R_{ij} = K \int_0^{2\pi} \int_0^{\pi} G_i \cdot \underline{C}_i(\theta, \psi) \cdot G_j \cdot \underline{C}_j^*(\theta, \psi) \cdot S(\theta, \psi) \cdot e^{jk\Delta\Phi(\theta, \psi)} \sin \theta \cdot d\theta \cdot d\psi$$

$$\sigma_{i,j} = \sqrt{K \int_0^{2\pi} \int_0^{\pi} G_{i,j} \cdot |C_{i,j}(\theta, \psi) \cdot G_{i,j}|^2 \cdot S(\theta, \psi) d\Omega}$$

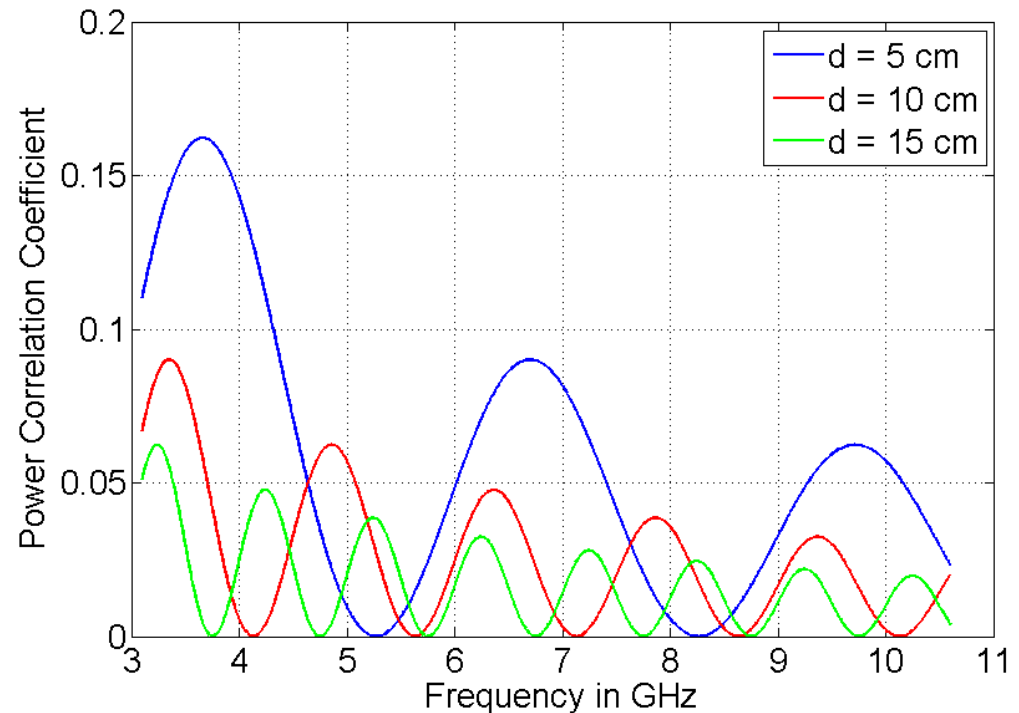
For an analytical evaluation an assumption on the incoming wave front distribution has to be made:

- e.g.
- incident waves from 360° in azimuth ψ
 - incidence in elevation θ : $90^\circ \pm 10^\circ$ Gauß distributed

4 element array



Isotropic elements
,worst case '
same polarization



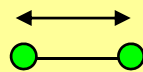
Assuming uniform 2D distribution of incoming waves:

$$\rho(d) = \int_0^{2\pi} \underbrace{C(\psi)}_{\equiv 1} \cdot \underbrace{C(\psi)}_{\equiv 1} e^{j2\pi d / \lambda \cdot \cos\psi} d\psi = \int_0^{2\pi} e^{j2\pi d / \lambda \cdot \cos\psi} d\psi = J_0(2\pi d / \lambda)$$

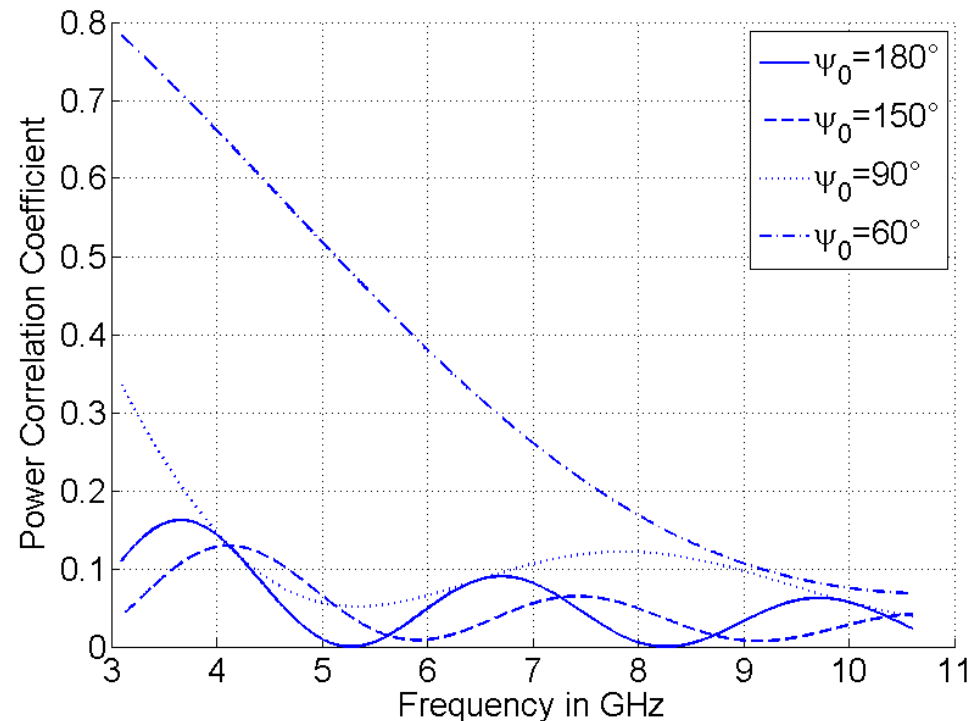
≡ 1 ≡ 1 for isotropic elements

2 elements

$d=5$ cm



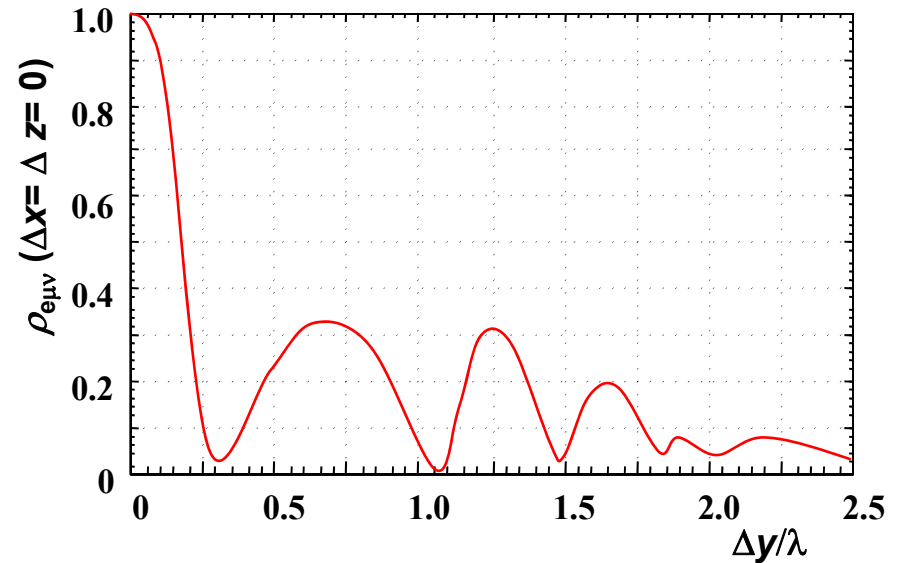
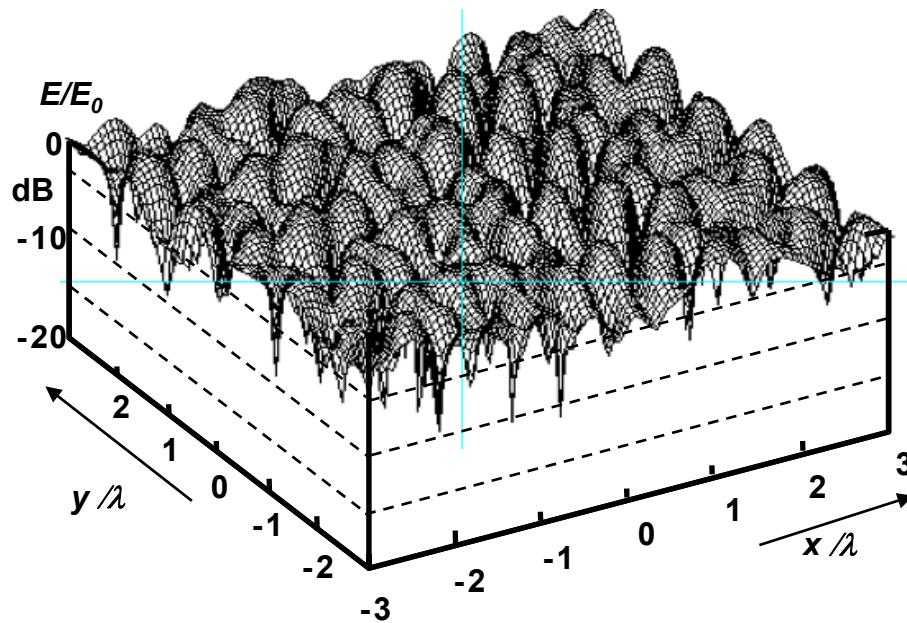
Isotropic elements
,worst case '
same polarization



Assuming uniform 2D distribution over a limited angular sector ψ_0 :

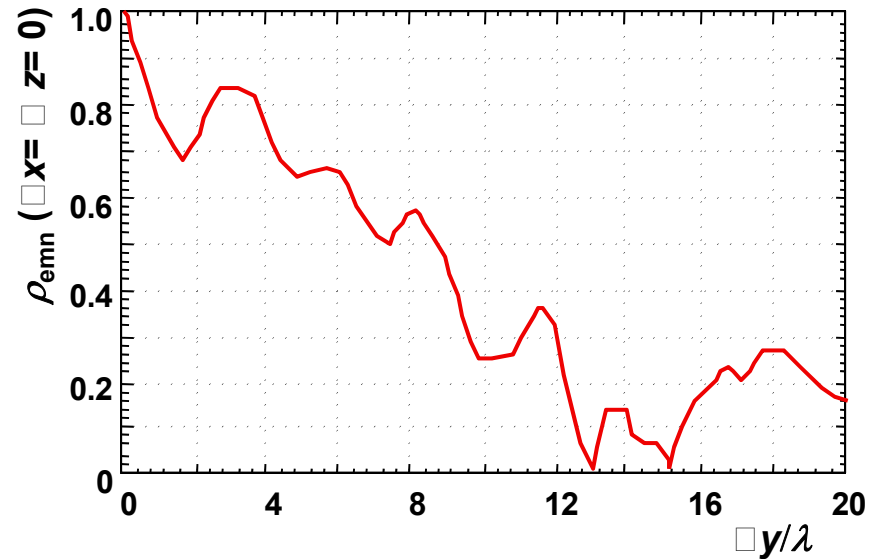
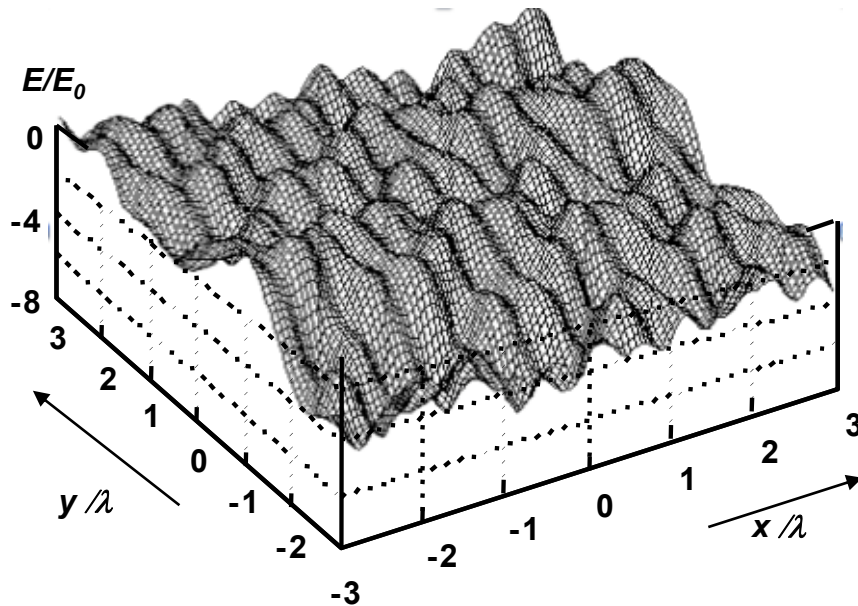
$$\rho(d, \lambda) = \frac{1}{\psi_0} \int_0^{\psi_0} e^{j2\pi d / \lambda \cdot \cos \psi} d\psi$$

Envelope Cross Correlation Coefficient



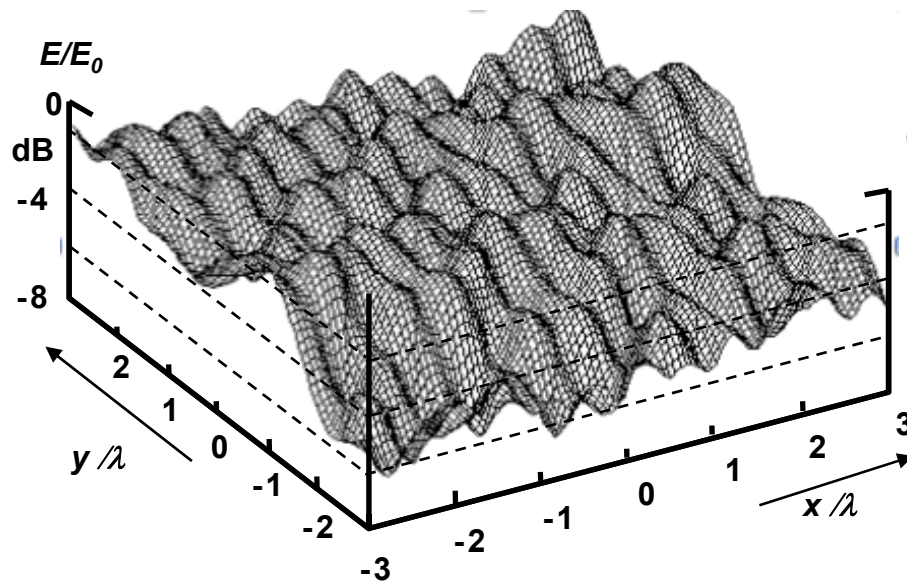
**urban environment, $\lambda/2$ -dipole,
vertical polarization, $f=925\text{MHz}$**

Envelope Cross Correlation Coefficient



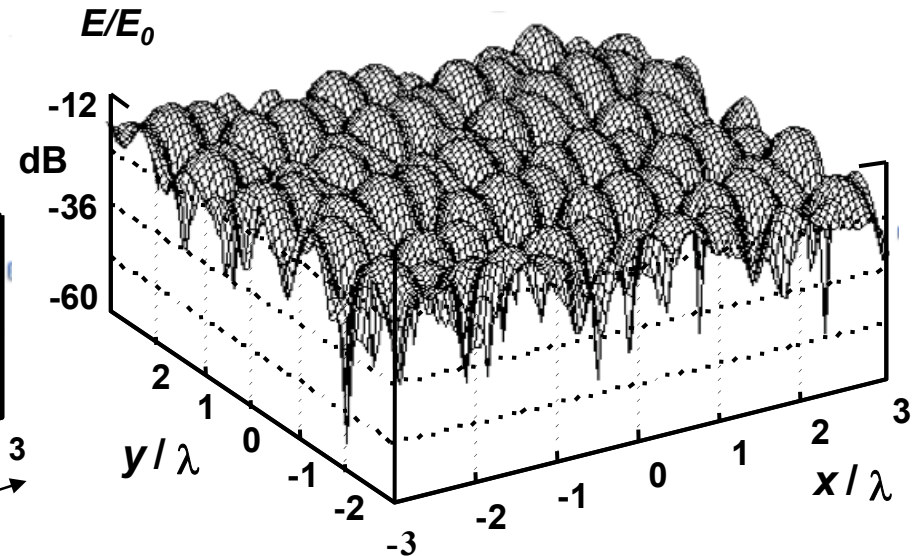
**hilly terrain, $\lambda/2$ -dipole,
vertical polarization, $f=925\text{MHz}$**

Hilly terrain, $\lambda/2$ -dipole



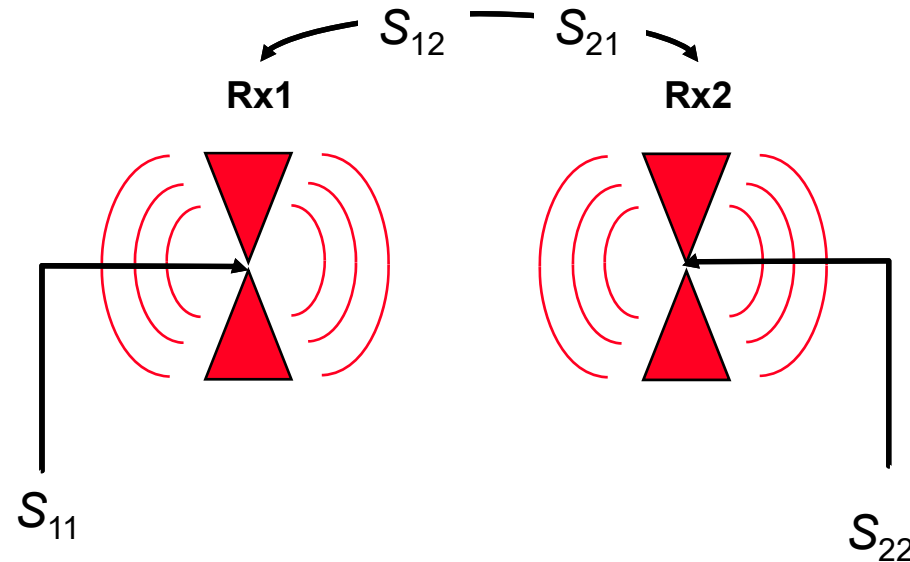
vertical polarization, $f=925\text{MHz}$
rel. average E/E_0 level = -3,8dB

Hilly terrain, loop antenna



horizontal polarization, $f=925\text{MHz}$
rel. average E/E_0 level = -27,1dB

$$\rho_{e12} = 0,34$$



$$\rho_{1-2} = \frac{|S_{11}^* S_{12} + S_{21}^* S_{22}|^2}{(1 - (|S_{11}|^2 + |S_{21}|^2)) \cdot (1 - (|S_{22}|^2 + |S_{12}|^2))}$$

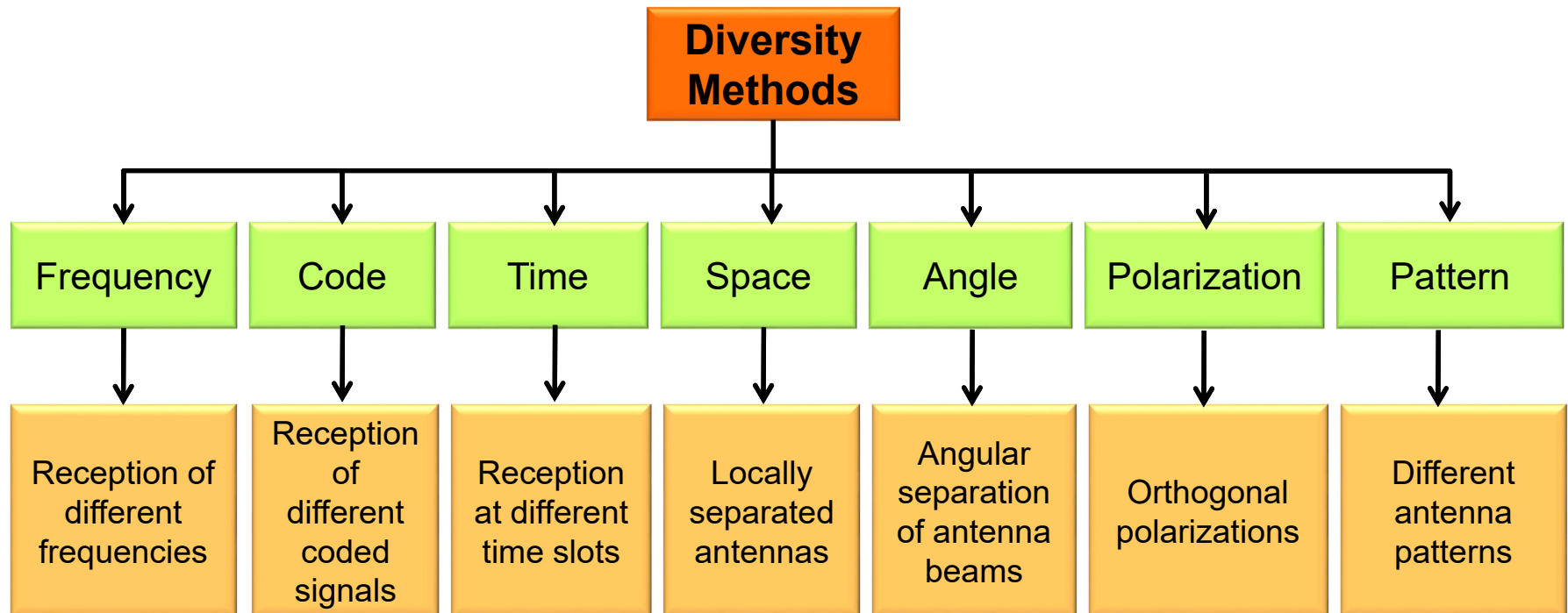
S. Blanch, J. Romeu, and I. Corbella, "Exact representation of antenna system diversity performance from input parameter description," *Electronics Lett.*, vol. 39, no. 9, pp. 705–707, May 2003.

Diversity Principles

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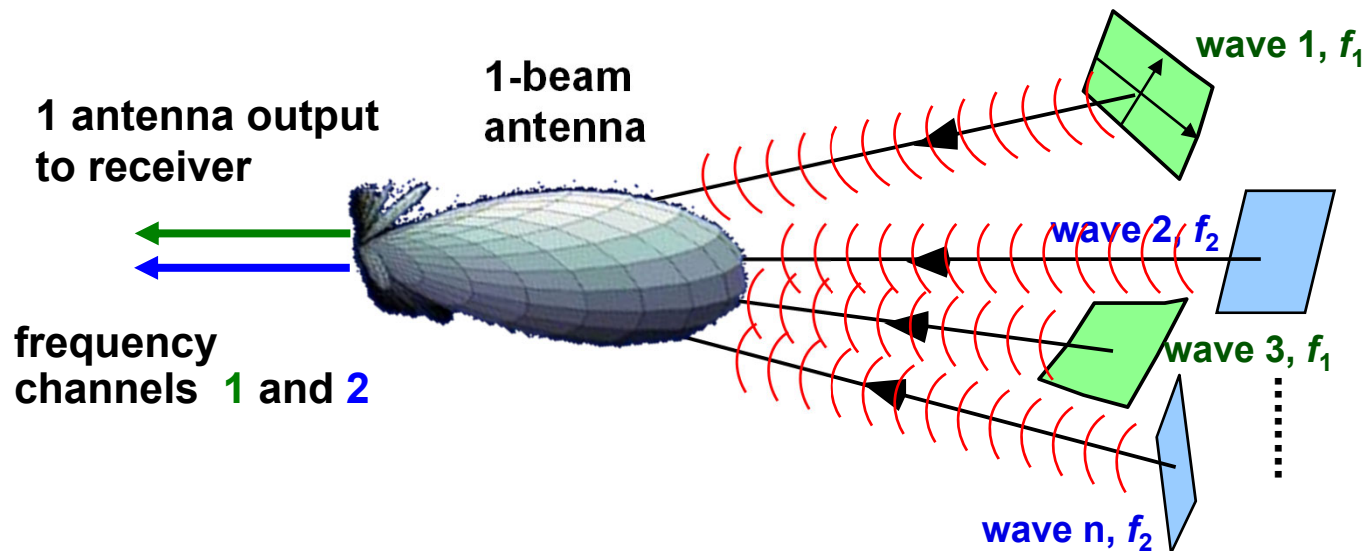


by Werner Wiesbeck and Christian Waldschmidt

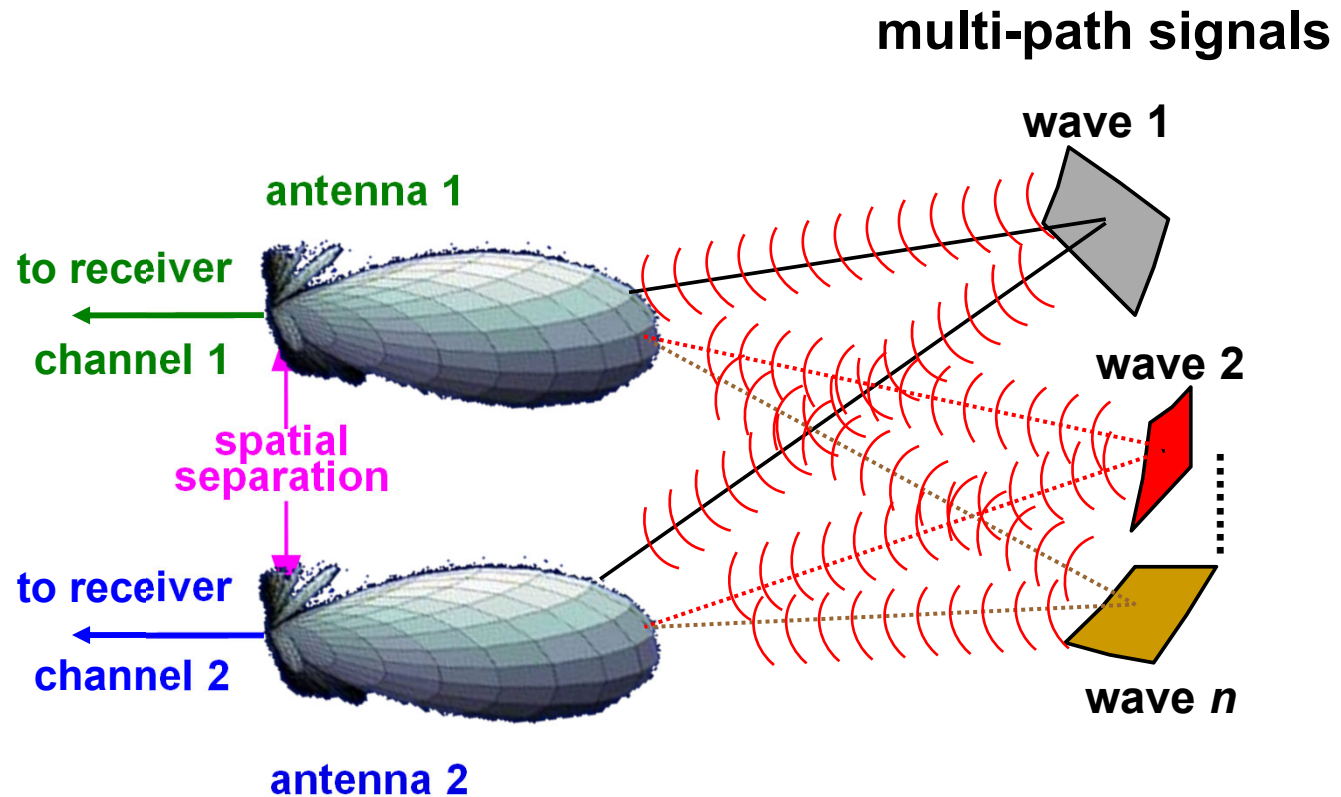


2 frequencies from one receiving antenna

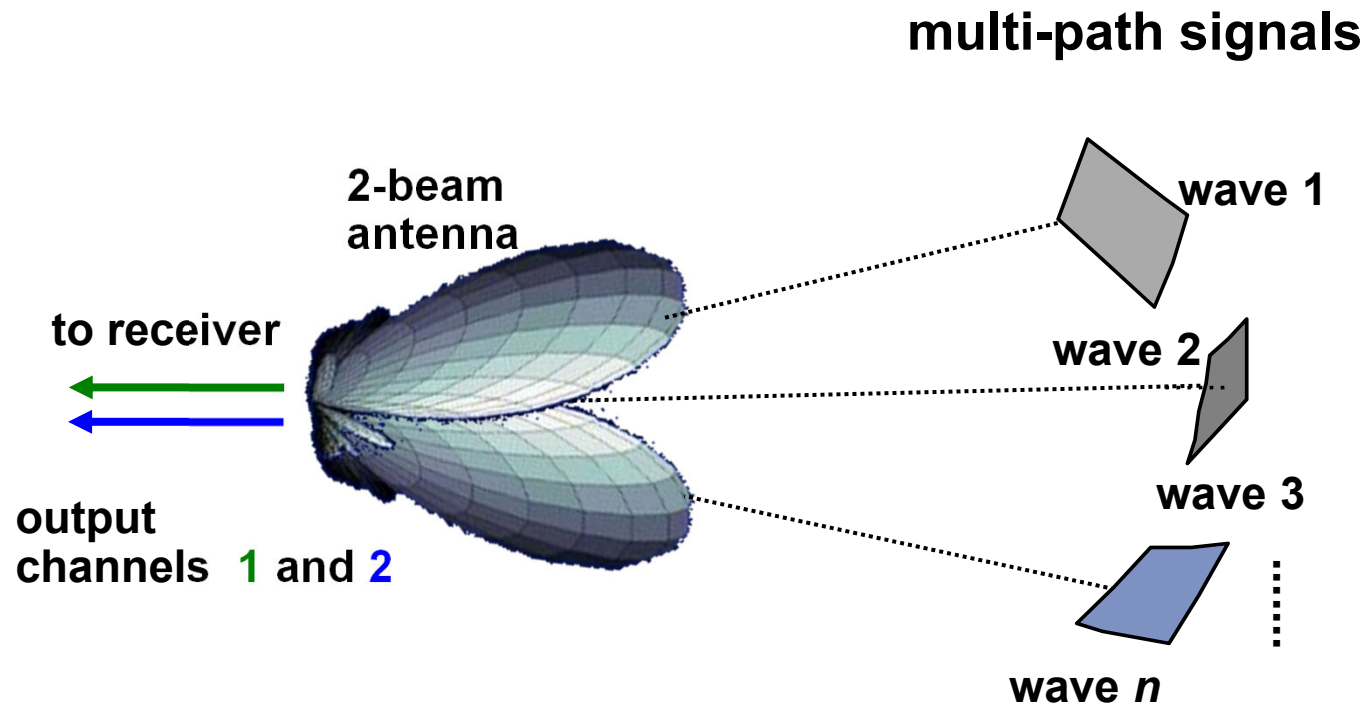
multi-path signals
at 2 frequencies



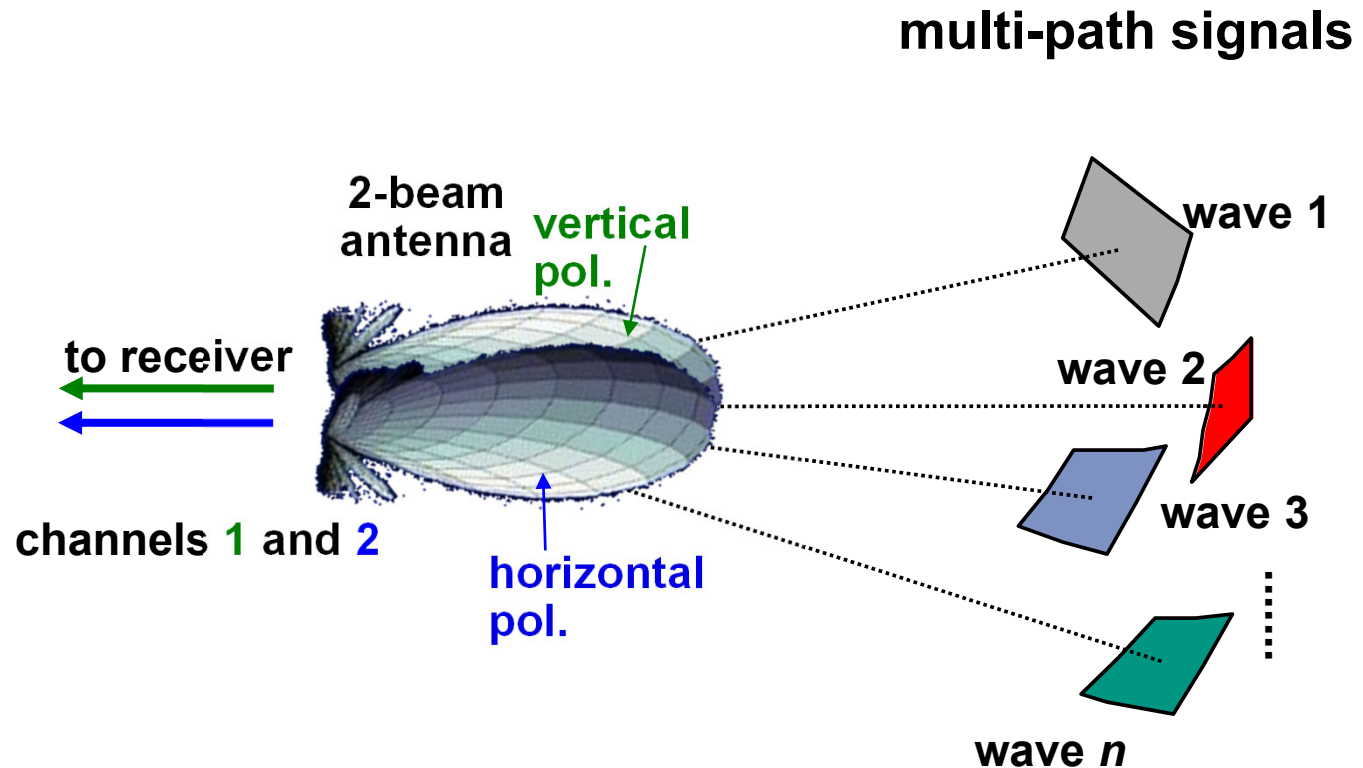
2 locally separated antennas



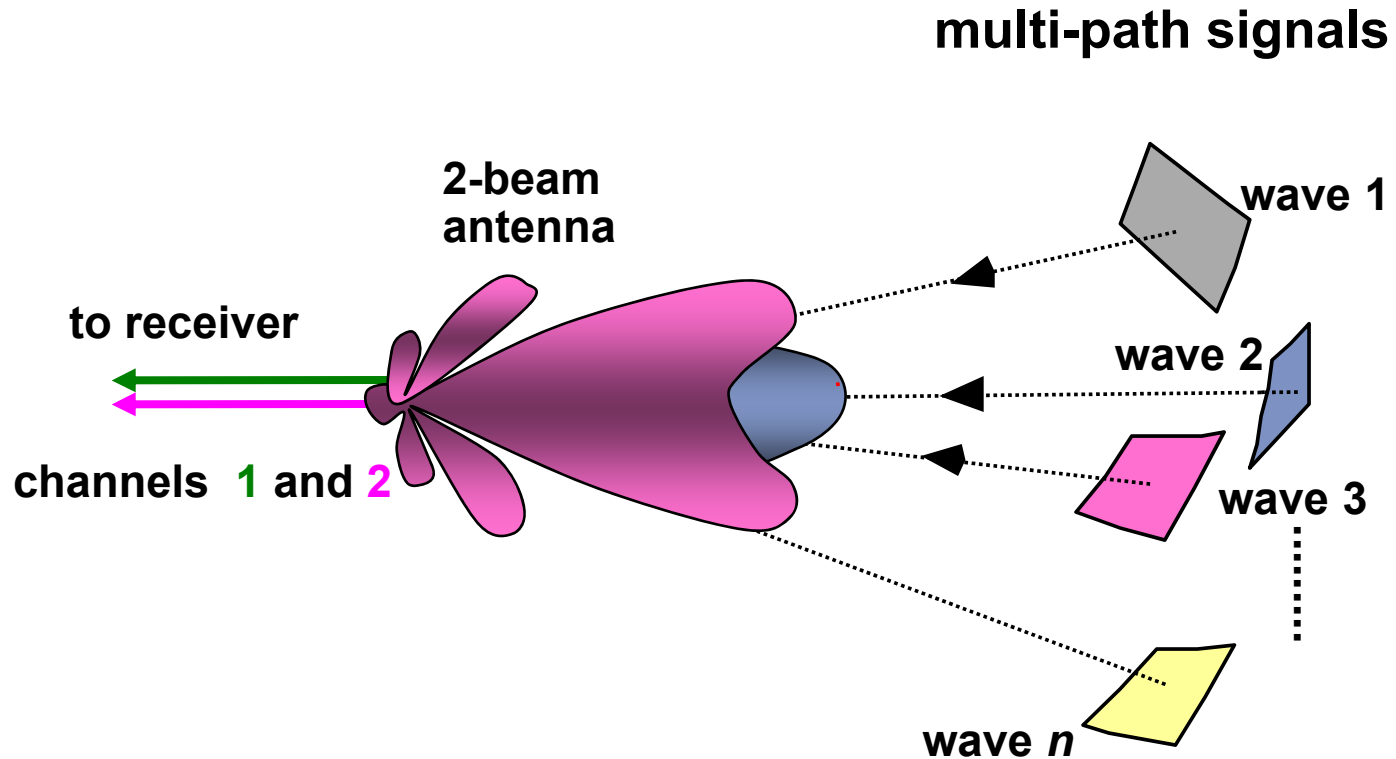
2 medium gain antennas, angular separation of app. 30°



2 linear orthogonal polarized antennas



2 different antenna patterns from one antenna



Diversity Methods for the **GSM** System

Diversity method	Technical possibility	Signal improvement	Size	Cost	Recommendation
Frequency diversity	--	++	+	-	--
Code diversity	--	++	+	-	--
Time diversity	--	++	+	-	--
Space diversity	+	+	0	-	+
Angle diversity	+	+	0	0	+
Polarization diversity	+	+	+	+	++
Pattern diversity	+	0	+	+	+

-- not possible; - bad; 0 medium; + good;

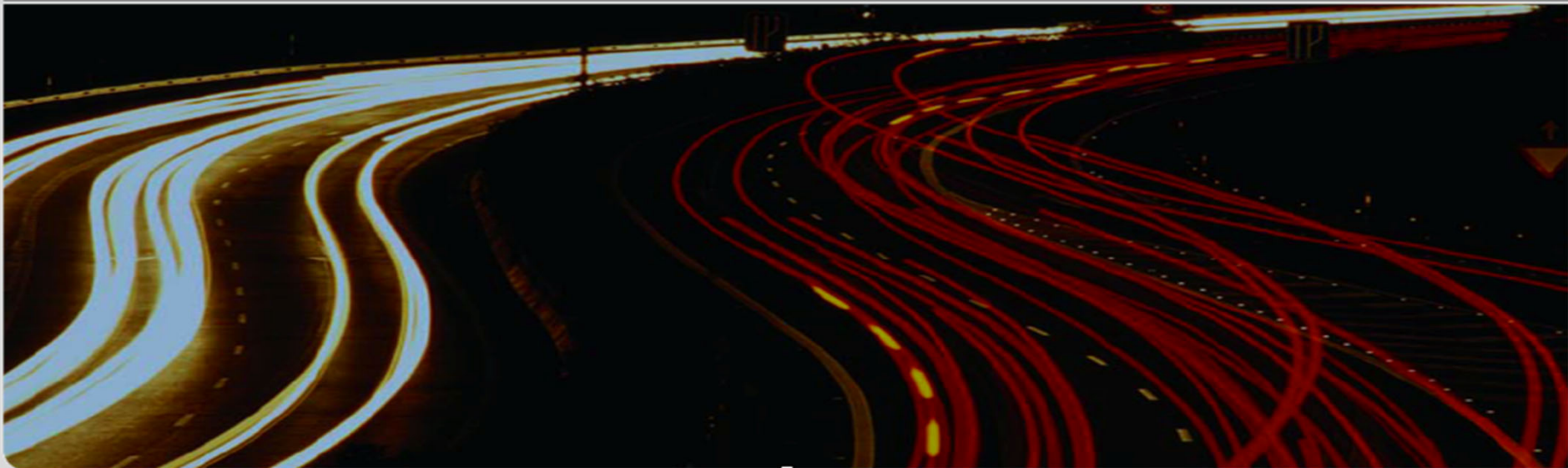
Diversity Methods for the Automotive **DAB** Radio

Diversity method	Technical possibility	Signal improvement	Size	Cost	Recommendation
Frequency diversity	+	++	+	+	++
Code diversity	--	++	+	--	--
Time diversity	--	++	+	--	--
Space diversity	+	++	0	0	+
Angle diversity	+	++	0	0	+
Polarization diversity	+	+	+	+	++
Pattern diversity	+	++	0	+	+

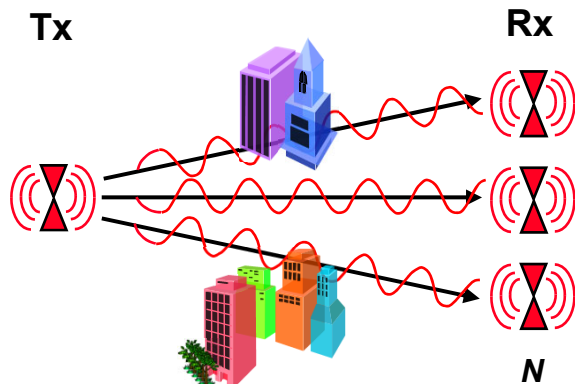
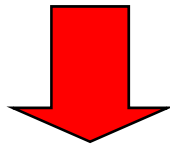
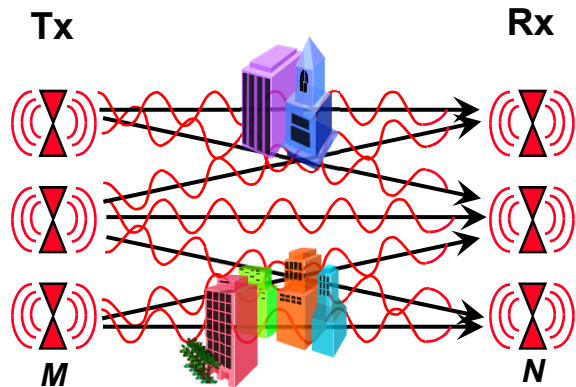
-- not possible; - bad; 0 medium; + good;

Diversity Combiner Principles

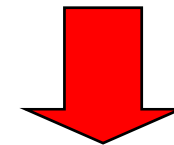
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Single Tx, N Rx: Classical Diversity

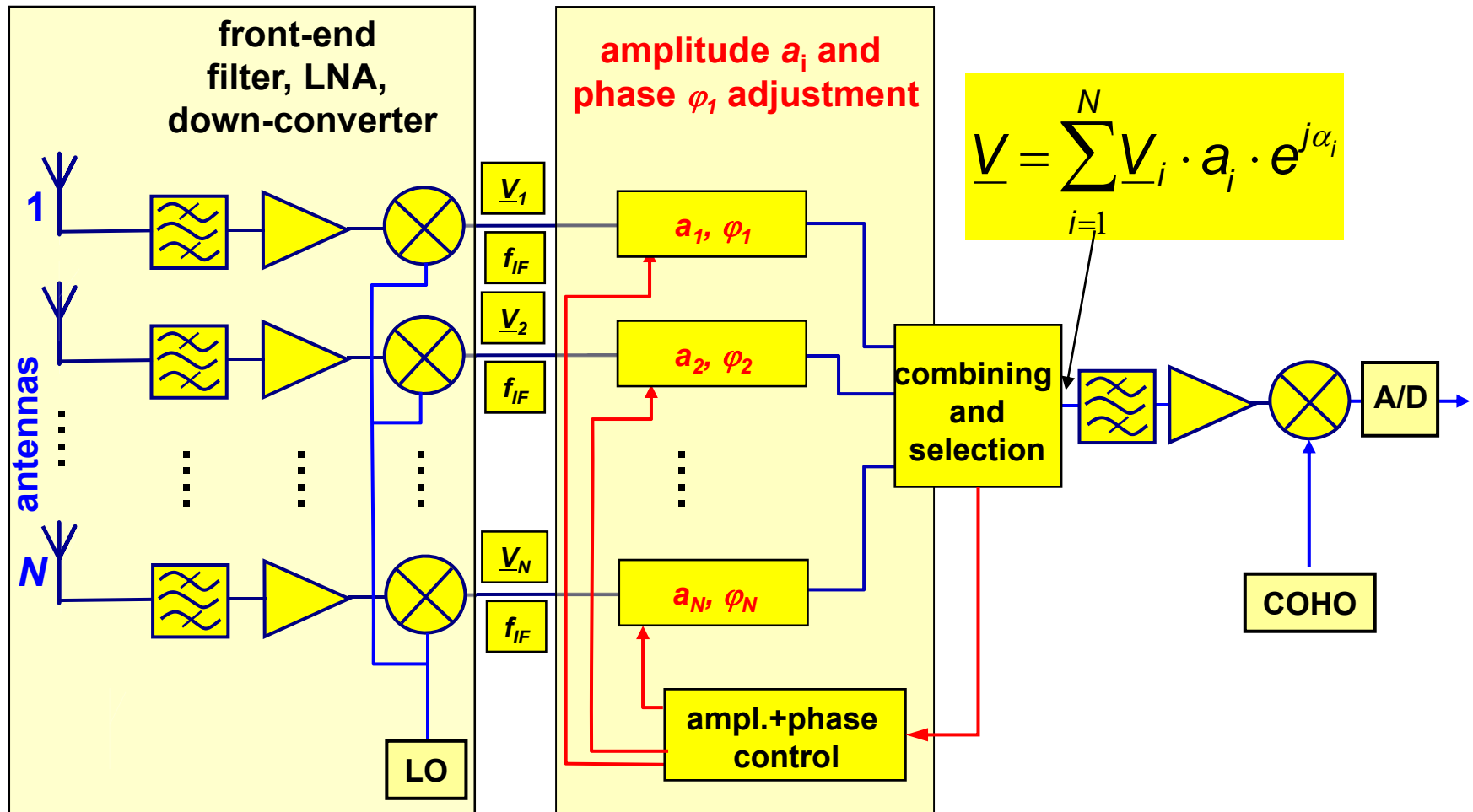


$$\mathbf{H} = \begin{pmatrix} H_{11} & H_{12} & \dots & H_{1M} \\ H_{21} & H_{22} & \dots & H_{2M} \\ \vdots & & \ddots & \vdots \\ H_{N1} & \dots & & H_{NM} \end{pmatrix}$$

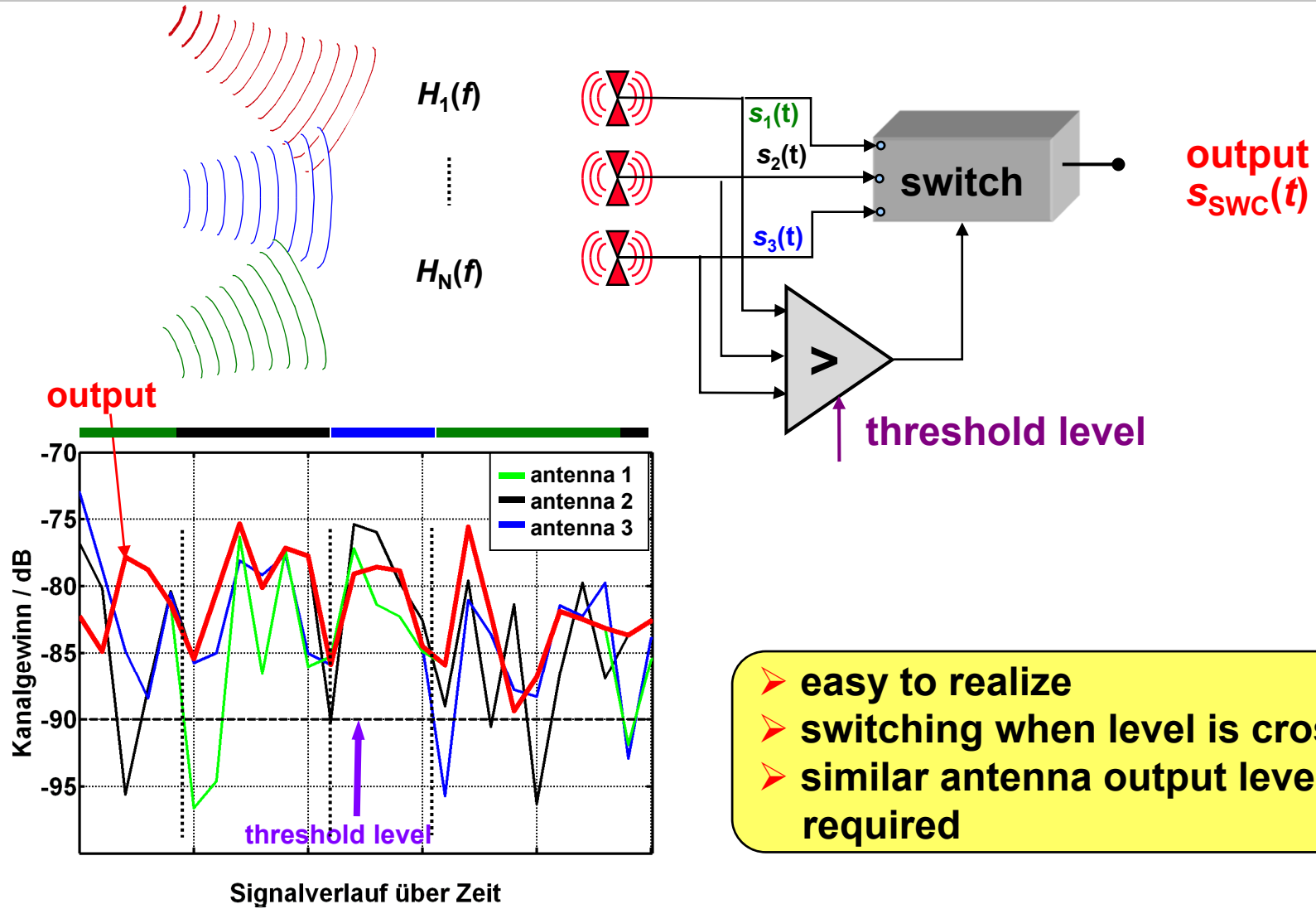


$$\mathbf{H} = \begin{pmatrix} H_1 \\ H_2 \\ \vdots \\ H_N \end{pmatrix}$$

Generic Block Diagram of a Diversity Receiver

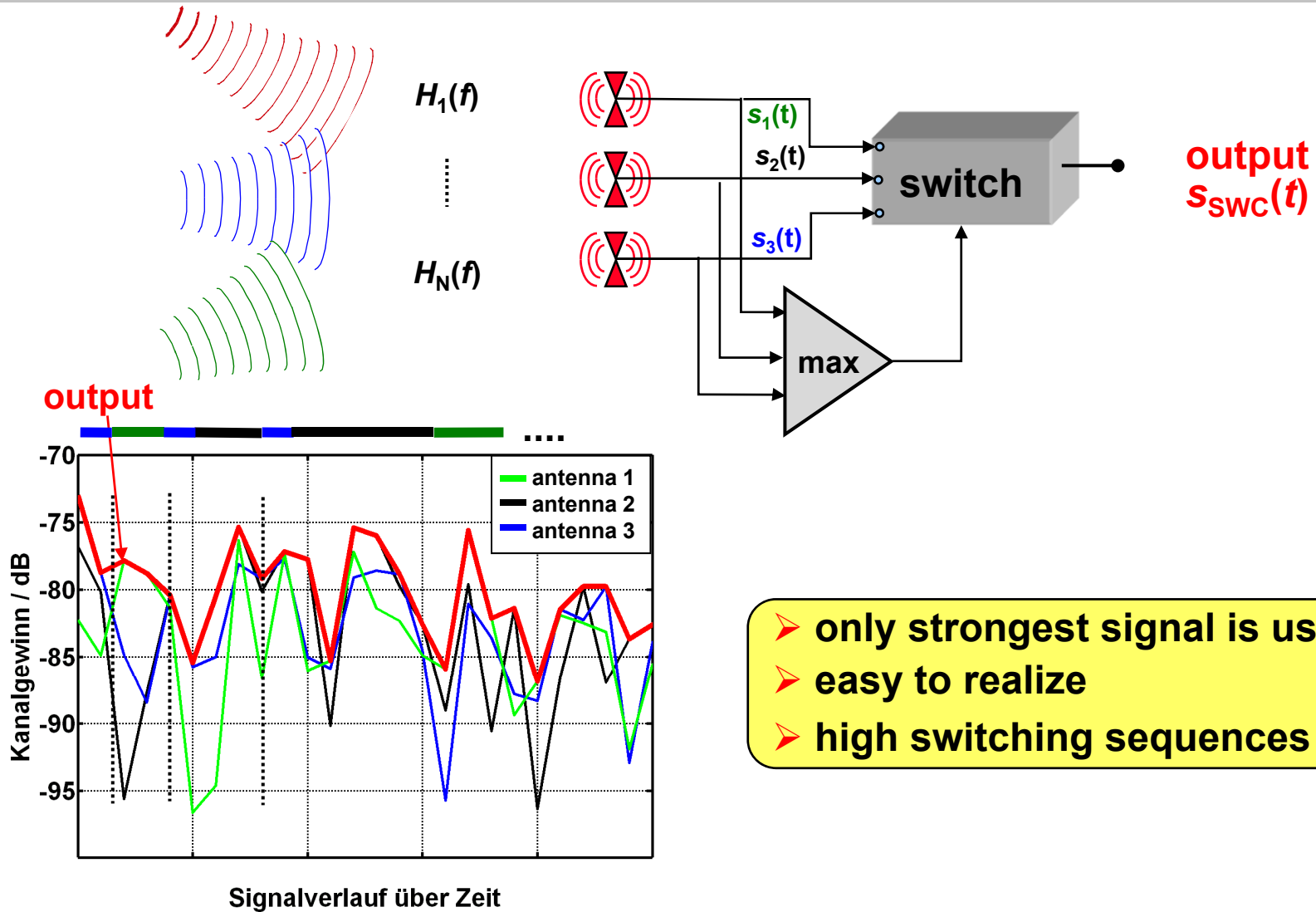


Switched (Selection) Combining (SWC)

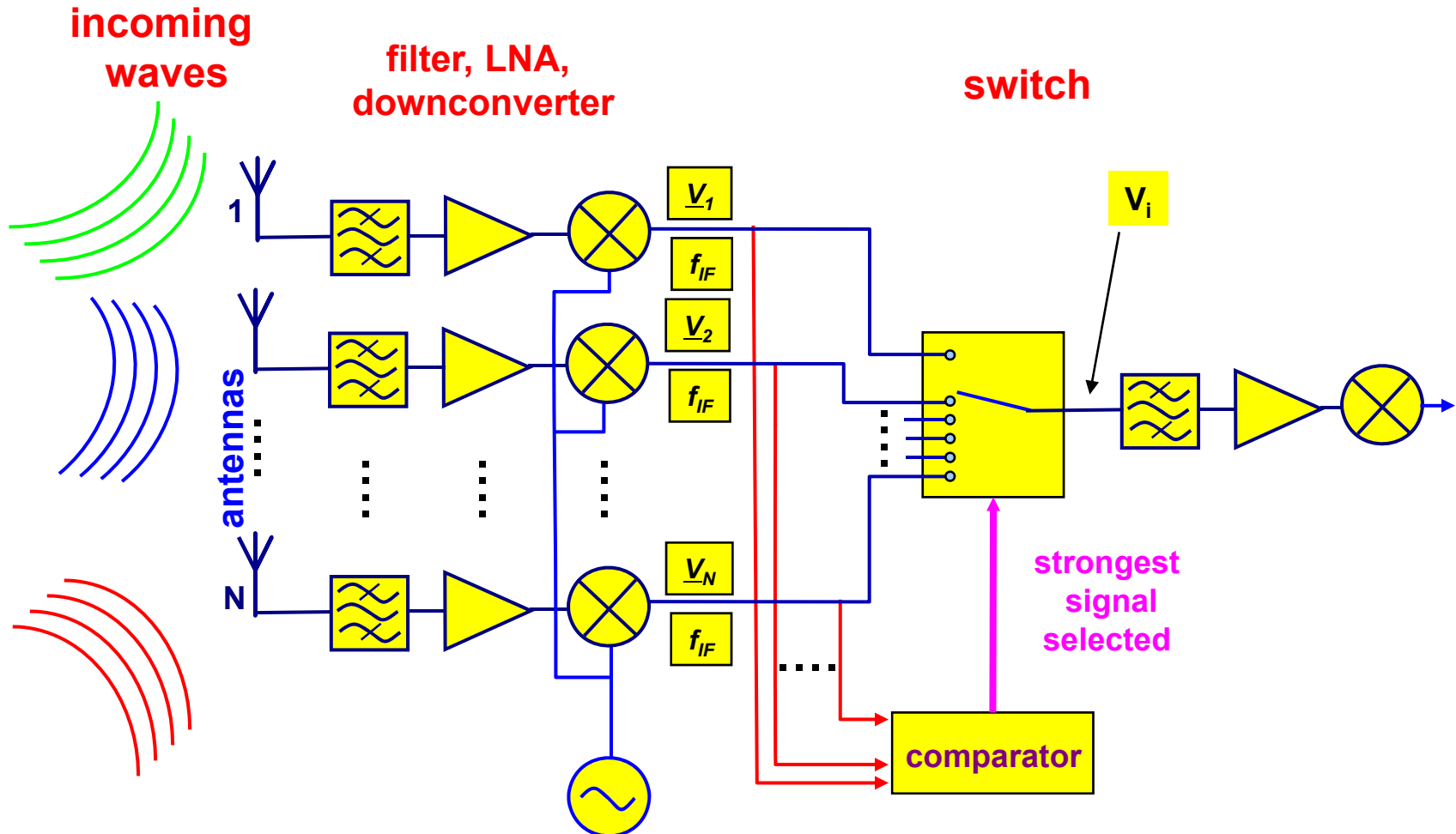


- easy to realize
- switching when level is crossed
- similar antenna output levels required

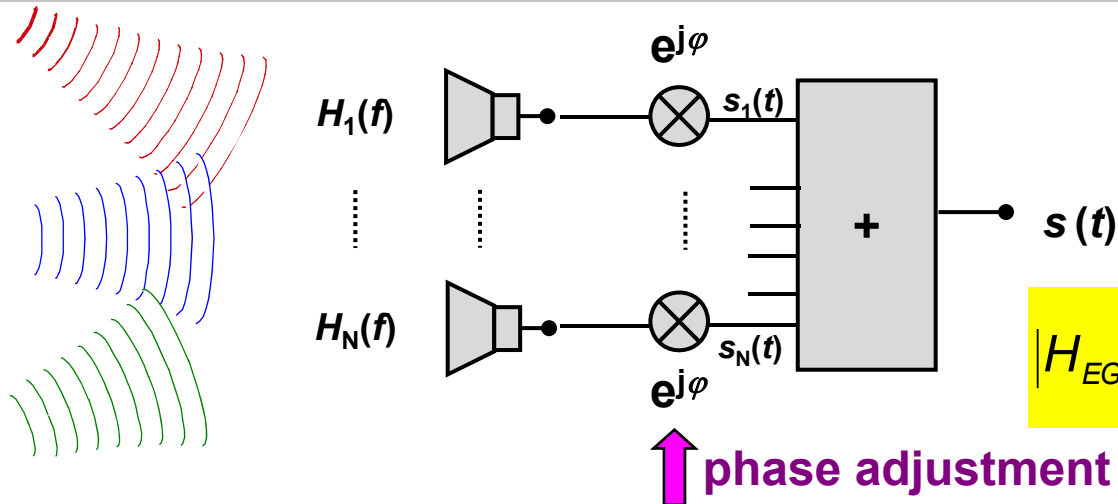
Selection Combining (SEC)



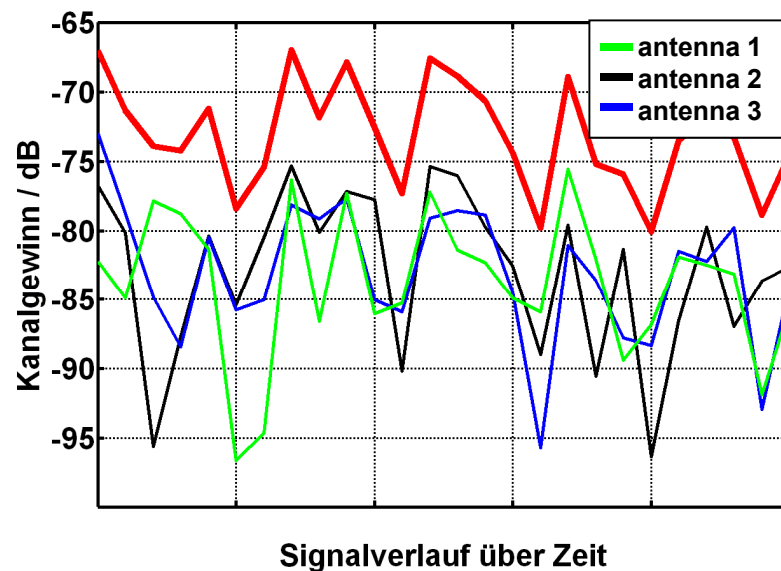
Selection Combining (SEC) Block Diagram



Equal Gain Combining (EGC)

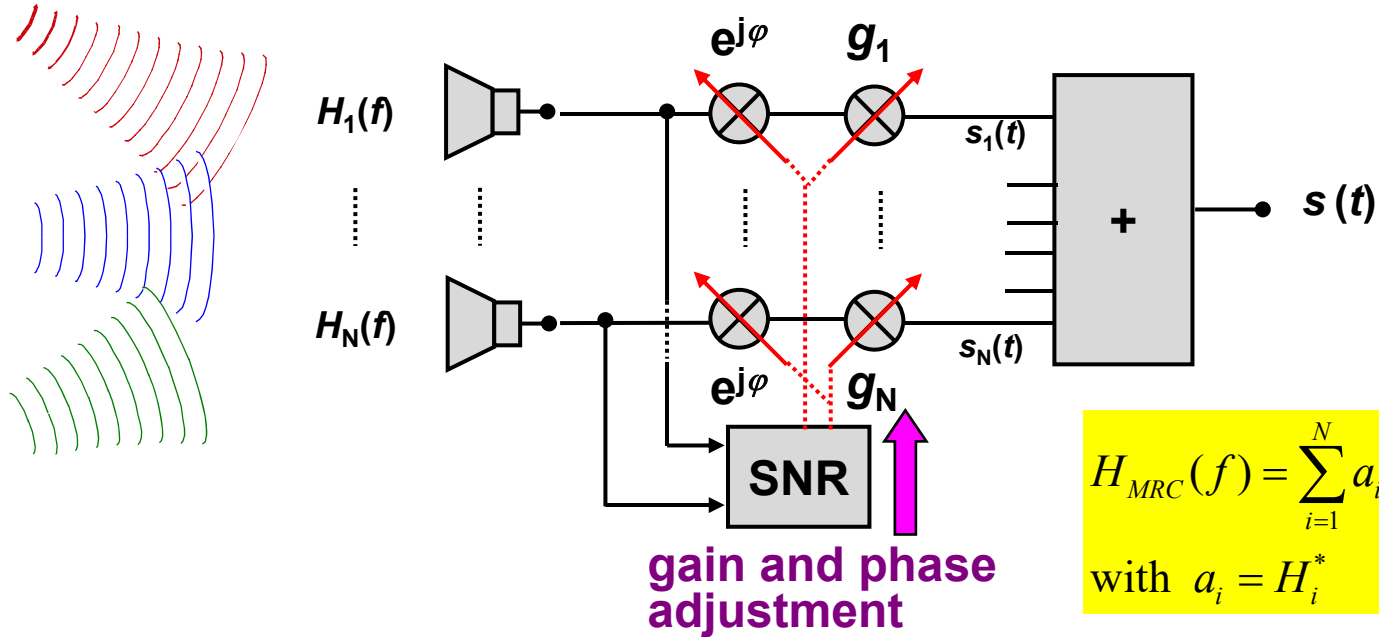


$$|H_{EGC}(f)| = \sum_{i=1}^N |H_i(f)|$$



- medium complexity
- phase shifters required
- all antenna signals identically weighted
- problem: noise summation

Maximum Ratio Combining (MRC)



$$H_{MRC}(f) = \sum_{i=1}^N a_i H_i(f)$$

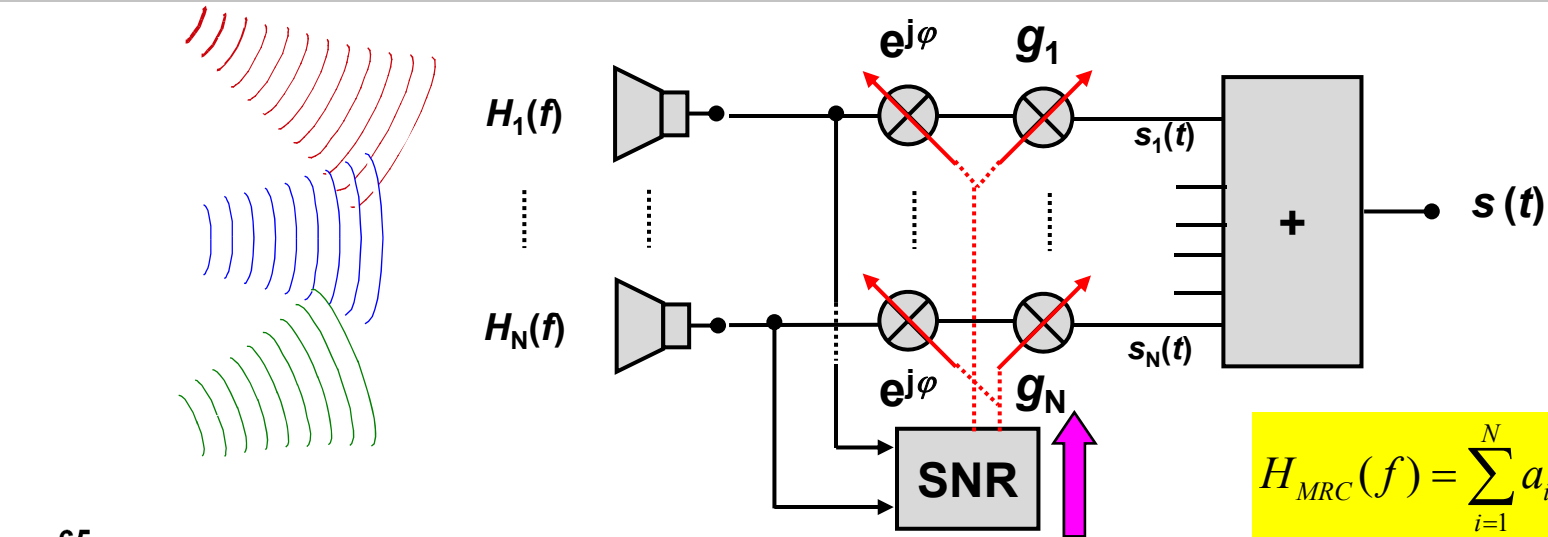
with $a_i = H_i^*$

$$SNR_i = \frac{|H_i|^2}{\sigma_n^2}$$

$$SNR_{MRC} = \frac{\left| \sum_{i=1}^N H_i a_i \right|^2}{\sigma_n^2 \sum_{i=1}^N |a_i|^2} = \frac{1}{\sigma_n^2} \sum_{i=1}^N |H_i|^2 \frac{\left| \sum_{i=1}^N H_i a_i \right|^2}{\sum_{i=1}^N |H_i|^2 \sum_{i=1}^N |a_i|^2}$$

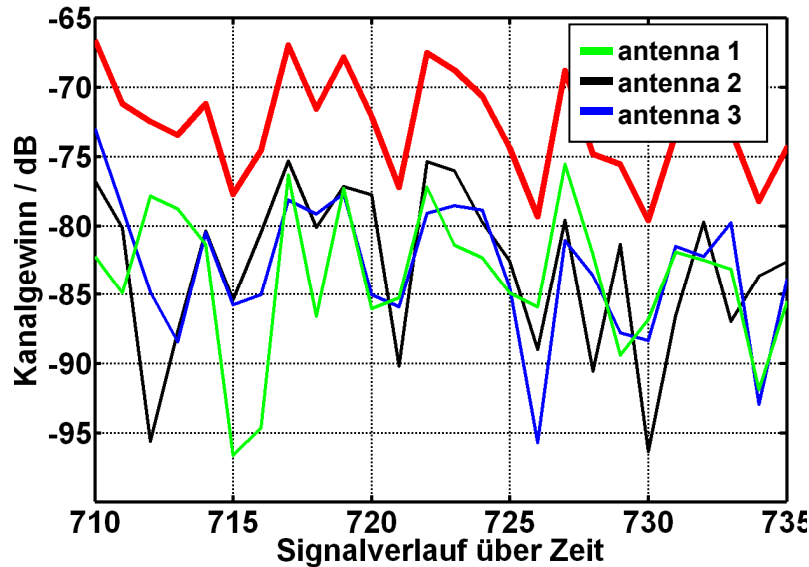
Cauchy-Schwartz: $\left| \sum_{i=1}^N H_i a_i \right|^2 \leq \sum_{i=1}^N |H_i|^2 \sum_{i=1}^N |a_i|^2$ equal for $a_i = H_i^* \Rightarrow SNR_{MRC} = \sum_{i=1}^N SNR_i$

Maximum Ratio Combining (MRC)



$$H_{MRC}(f) = \sum_{i=1}^N a_i H_i(f)$$

with $a_i = H_i^*$

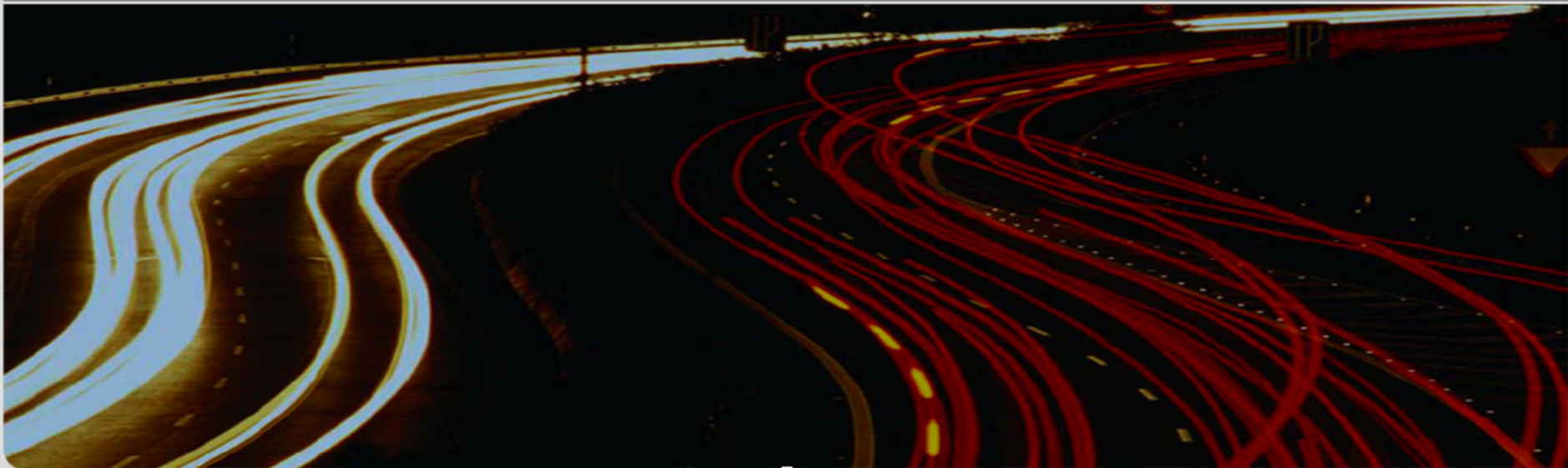


gain and phase adjustment

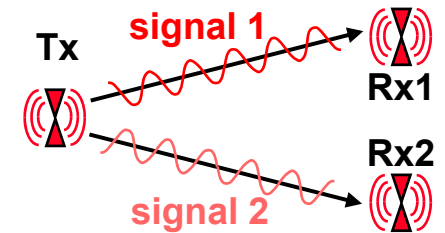
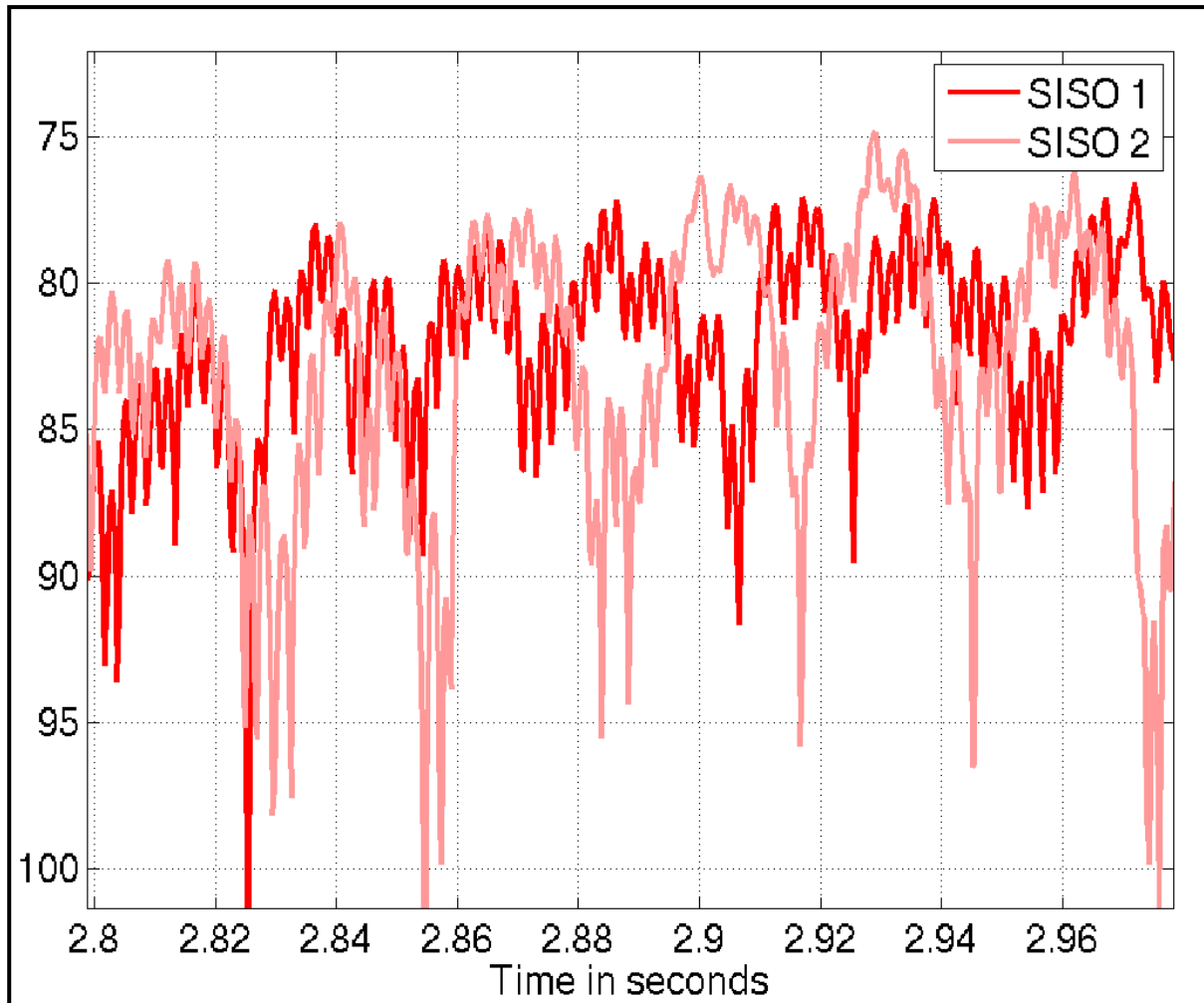
- high complexity
 - phase shifters
 - controlled amplifiers
- signals of all antennas weighted according to their SNR

Diversity Systems Comparison

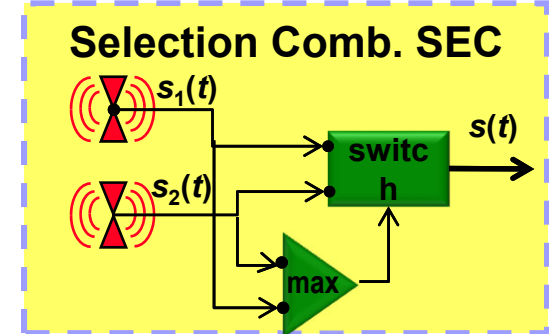
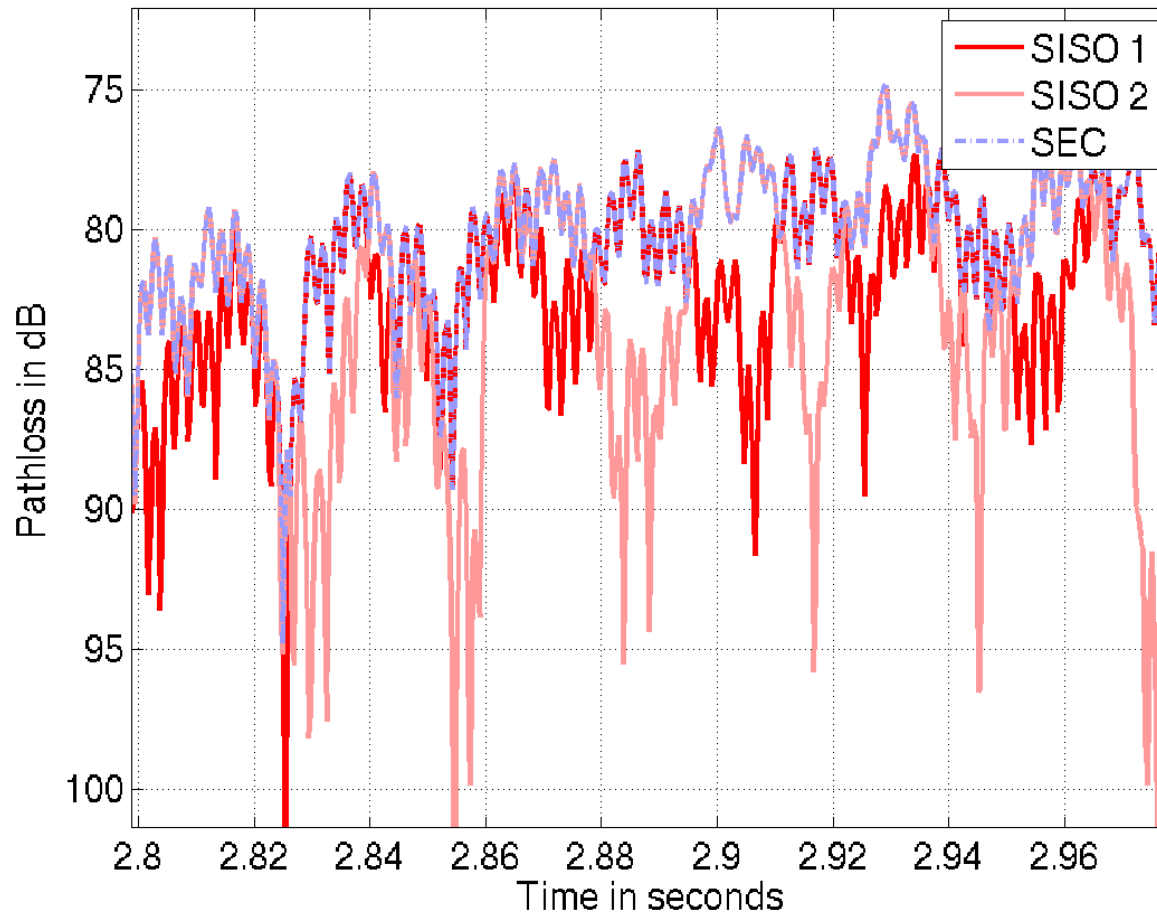
Institut für Hochfrequenztechnik und Elektronik



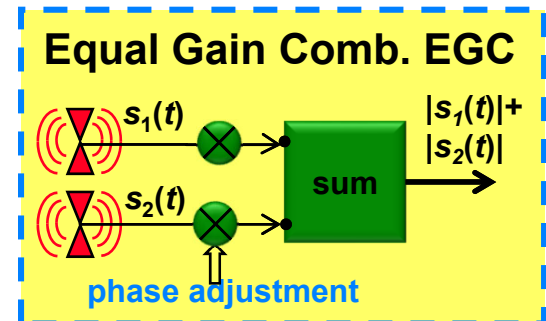
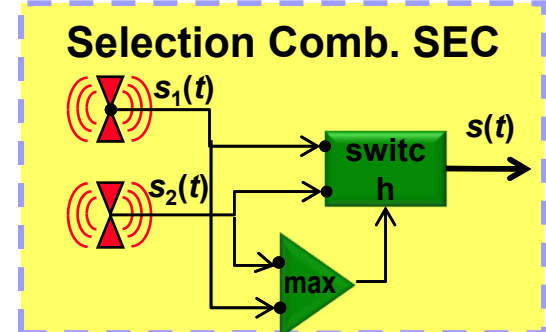
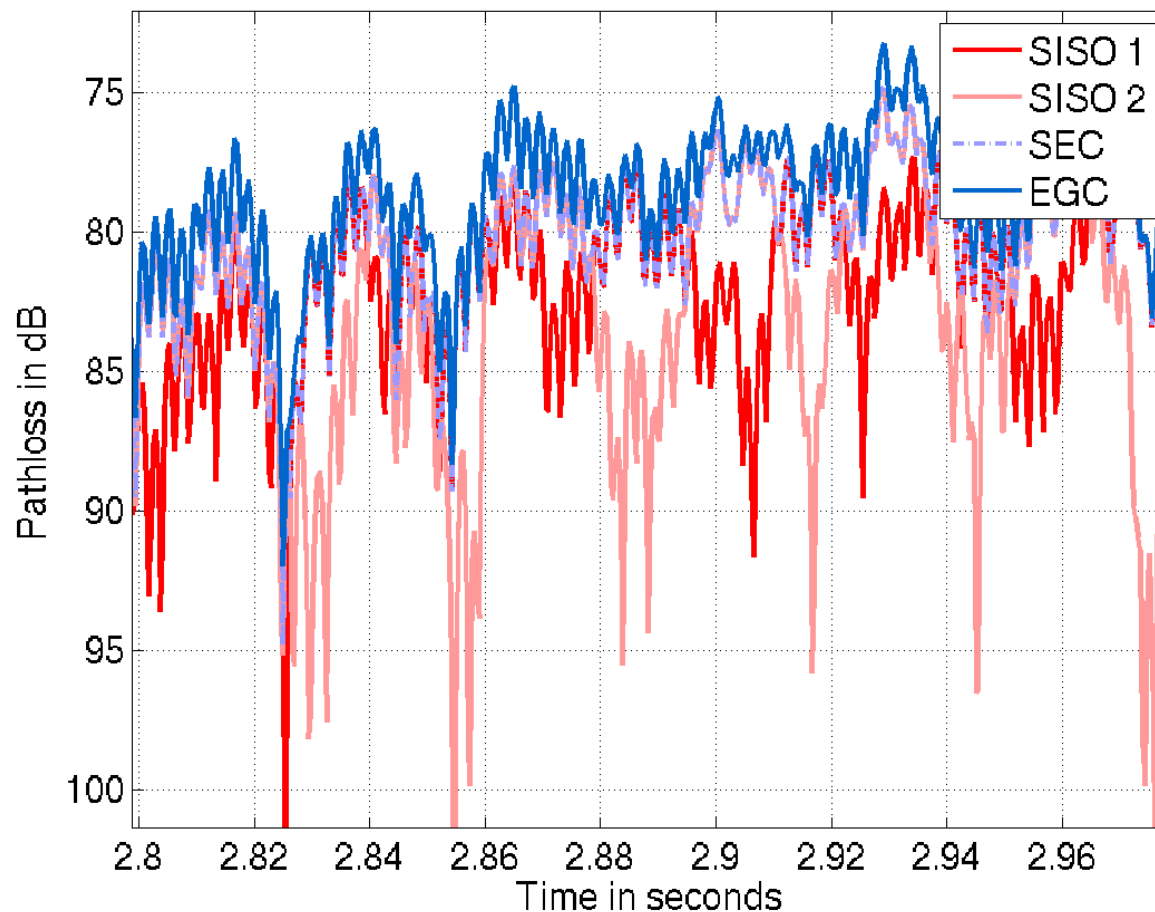
Use of Multiple Antenna Systems



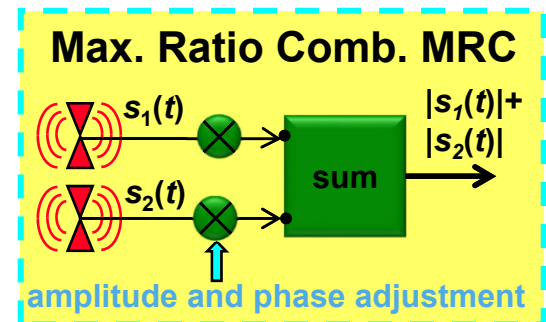
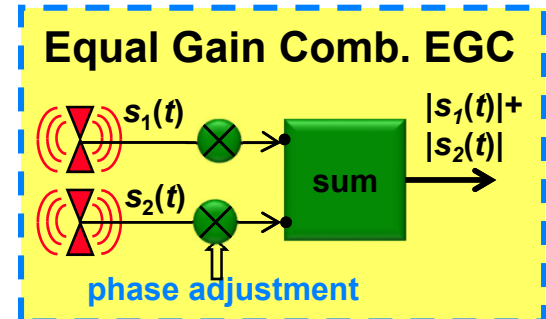
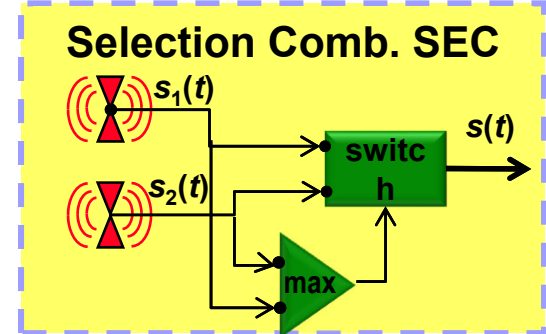
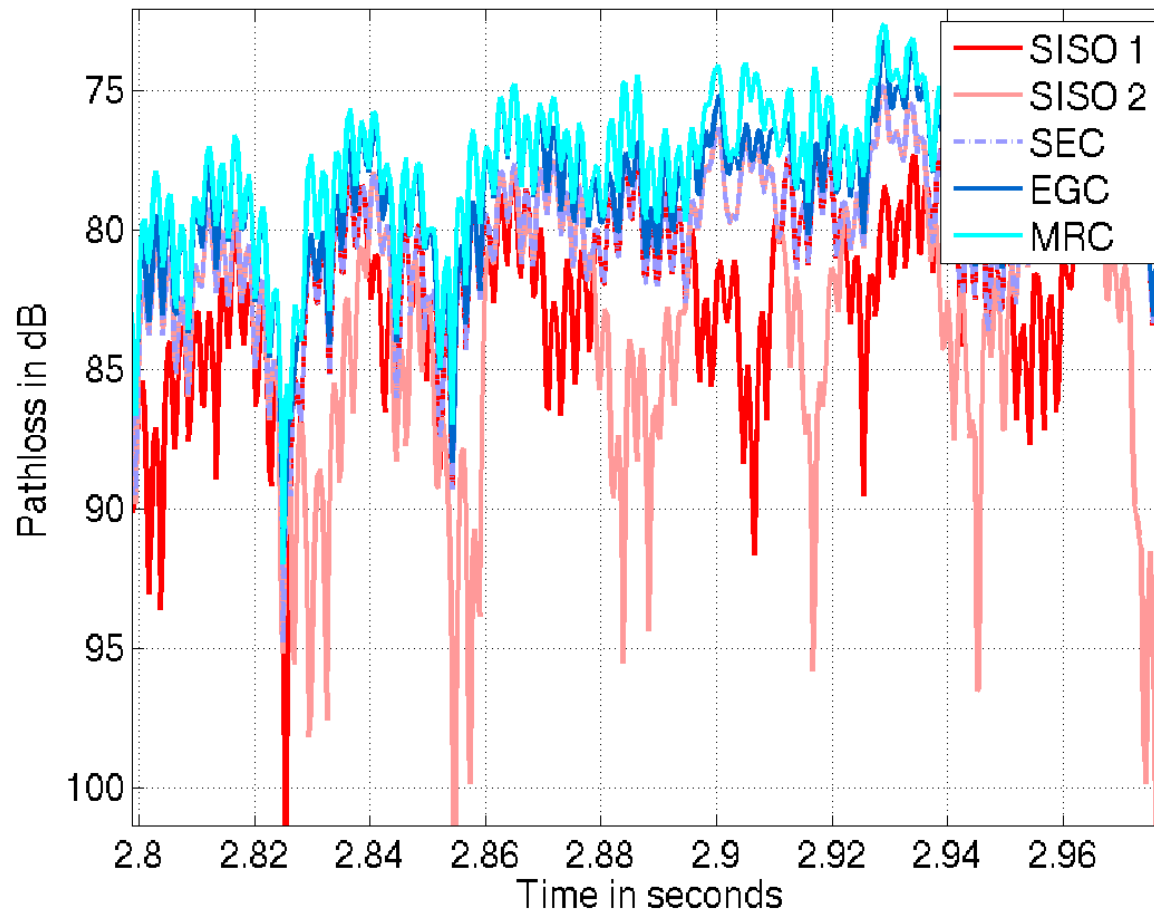
Diversity- Selection Combining (SEC)



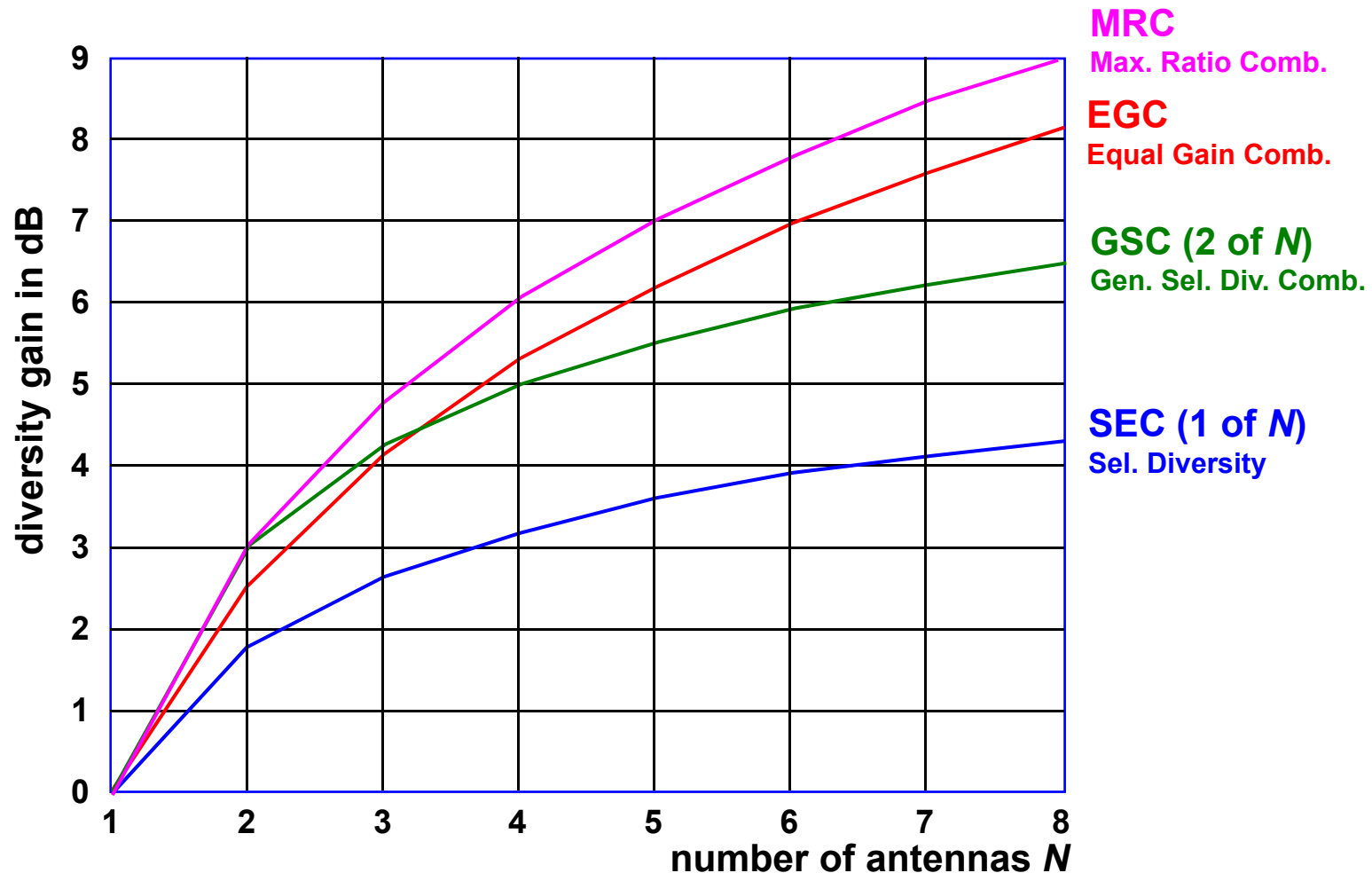
Diversity Comparison: Selection-Equal Gain



Diversity Comparison: Selection-Equal-Gain- Max Ratio



Upper SNR-Bound for Diversity Schemes



Channel: Nakagami fading channels

- **Patent: DE 102005061723.9 Verfahren zum Empfang von Antennensignalen mindestens zweier Empfangsantennen eines Antennensystems und Antennensystem**
- **DE 38 36 046 C2**
- **EP 1 126 631 B1**
- **DE 101 16 964 A1**
- **DE 38 02 130 2.1**
- **DE 38 02 131 2.1**

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